# VIBRATION OF A CLASS OF ORTHOTROPIC PLATES

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DEPARTMENT OF AERONAUTICAL ENGINEERING

INDIAN INSTITUTE OF TECHNOLOGY KANPUR JANUARY, 1976

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# VIBRATION OF A CLASS OF ORTHOTROPIC PLATES

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INDER KRISHEN PANDITTA

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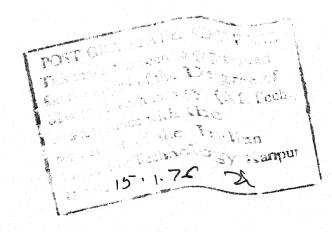
Certified that the work titled "Vibrations of a Class of Orthotropic Plates" has been carried out und ex my supervision and has not been submitted elsewhere for degree.

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#### ABSTRACT

The vibrations of orthotropic cantilever and free-free plate have been studied using Rayleigh-Ritz method.

The convergence of Rayleigh-Ritz method and the effect of different plate parameters have been investigated.

Calculations for frequency parameter has been carried out for five ratios of Young's modulus each incorporating five pois constant and ten aspect ratios. These have been tabulated and can be used for design purposes. These design tables contain first two modes of cantilever plate and first mode of free-free plate.

#### NOMENCLATURE

X, Y = Cartesian co-ordinates in the plane of plate

a = Plate dimension perpendicular to built in edge

b = Plate dimension parallel to built in edge

h = Plate thickness

W = Plate deflection normal to X-Y plane

 $\varepsilon_{v}$  = Normal strain in x-direction

 $\varepsilon_{y}$  = Normal strain in y-direction

 $\gamma_{xy}$  = Shear strain in x-y plane

 $\tau_{xy}$  = Shear stress in x-y plane

 $\sigma_{x}$  = Normal stress in x-direction

 $\sigma_{y}$  = Normal stress in y-direction

 $E_x$  = Young's modulus in x-direction

 $E_{y}$  = Young's modulus in y-direction

 $D_{i} = E_{i}/(1 - \sqrt[4]{x} v_{y})$ 

ω = Circular frequency

 $v_{x}$  = Pois**s**on's ratio in x-direction

 $\mathbf{v}_{\mathbf{v}}$  = Poiston's ratio in y-direction

# CHAPTER 1 INTRODUCTION

#### 1.1 Introduction:

The advent of advanced fiber re-inforced composite materials such as boron-epoxy and graphite-epoxy with their high potential weight savings and frequent applications in several fields of technology — Aerospace industry; Civil, Mechanical and Ocean engineering, etc. — have generated the need of sound understanding of the static and dynamic behaviour of anisotropic structures. A number of methods are available for predicting the dynamic response of the systems but the knowledge of natural modes and natural frequencies of the system is required by most of them.

An exact solution of the differential equation of a vibrating plate is known for the case of a rectangular plate which is simply supported along one pair of opposite edges with any conditions at the other two edges. For other combinations of edge conditions the solutions are more complicated, and it has been necessary to resort to various approximate methods — Rayleigh-Ritz being one of them.

While Rayleigh-Ritz method is well known, it has not been used as much as might be expected for plate

vibration problems. There appears to be little published data for the vibrations of rectangular orthotropic plate. This is probably due, at least in part, to the great amount of computational labour which is required both to set up and to solve the necessary equations. The amount of computation involved depends to a large extent upon the set of functions that is used to represent the plate deflections. For these functions some investigators (1,2) have taken series of polynomials while others (2,7) have used combinations of the characteristic functions which define the normal modes of vibration of a uniform beam.

#### 1.2 Historical Preview:

In 1966 Laura and others (1) used Galerkins method for calculating natural frequencies of rectangular plate clamped at all edges. First four frequencies were calculated for different b/a (a > b) and were put in a tabular form.

In 1973 Maurizi and Laura (2) made use of simple polynomial approximation for the determination of natural frequencies of clamped orthotropic plate. Galerkins method was used to investigate the effect of the rotation of material elastic axis with respect to natural co-ordinate system.

Young (3) used Ritz method for calculating frequencies of transverse vibration of an isotropic plate with different boundary conditions. Beam functions were employed to represent the plate deflection.

In 1969, Ashton and Anderson (4) worked on the natural frequencies of the laminated boron-epoxy plate with fully fixed boundary conditions.

Almost simultaneously Ashton (5) published his work on natural frequencies of free rectangular plate laminated of orthotropic plies. His work mostly concentrates on the stability problem. The solutions which illustrate the effect of plies and staking sequence, have also been presented. The results are not quite agreeing with experimental values.

In 1971, Mohan and Kingsbury (6) used Galerkin's method for plate with different boundary conditions. They used beam functions. Galerkins method, as they have used it, is good for obtaining mode shapes and natural frequencies of a plate with supported edges but can not be used for a plate with free edges, where the free edge zero bending moment and Krischoff's shear force conditions are not satisfied.

Bassily and Dickson (7) brought out the difference between Galerkin's and Rayleigh-Ritz method clearly and developed a Generalised Galerkin's approach in which the residual boundary forces and moments have been accounted for. But, unfortunately, while carrying out the theoretical analysis they have consistently missed the co-efficients  $C_{11}$  and  $C_{22}$  of  $(\frac{\epsilon_1}{a})^4$  and  $(\frac{\eta_k}{b})^4$  respectively in their equations (3) and (5), hence rendering their numerical results useless.

#### 1.3 Present Work:

In the present work Rayleigh-Ritz method has been employed for analysing the vibrating cantilever and free plate, as closed form solutions are almost impossible. In the application of Rayleigh-Ritz method a series in which each term is a product of normal beam functions has been used. For a plate with clamped edges the appropriateness of the normal functions of beam is apparent. Each term in the series satisfies boundary conditions of the plate and the determination of co-efficients by the minimization process brings about an approach to satisfaction of the differential equation. But, when the edges of the plate are free, as in our case, the normal functions of a beam with free ends do not give terms in the series which each

satisfy the free-edge boundary conditions of the plate. The beam functions will have vanishing second and third order derivatives. The satisfaction of the free-edge plate conditions requires non-zero values of corresponding derivatives. The plate boundary conditions thus remain to be satisfied by the series as a sum. The minimization process in relied on for this as bringing about an approach to the satisfaction of natural boundary conditions.

A generalised computer programme has been worked out in which (a) number of materials (b) number of terms in the series of beam functions (c) aspect ratios with fixed step size (d) modal frequency numbers (e) symmetry, antisymmetry of the problem involved can be controlled by merely changing the appropriate data cards.

With the help of this programme convergence of Rayleigh-Ritz method; effect of aspect ratio, poisions ratio and ratio of Young's modulus of the plate have been investigated. Few design tables have also been presented.

#### CHAPTER 2

#### THEORETICAL ANALYSIS

#### 2.1 Introduction:

In this chapter equations for vibrations of orthotropic plate are developed and the method of solution is discussed.

#### 2.2 General Theory:

The approximate theory for bonding of a plate based on Krischoff's hypothesis — reactilinear sections which in the undeformed plate were normal to the middle surface remain rectilinear and normal to the bent middle surface (OR  $\varepsilon_{\rm Z}=\gamma_{\rm XZ}=\gamma_{\rm yZ}=0$ ). And normal stress acting on planes parallel to mid surface are small compared to other stresses and can be neglected (OR  $\sigma_{\rm Z}=0$ ) — leads to the following strain-displacement relations:

$$\varepsilon_{x} = \frac{\partial u}{\partial x} = -z \frac{\partial^{2}w}{\partial x^{2}} \qquad . . . 2.1a$$

$$\varepsilon_{y} = \frac{\partial u}{\partial y} = -z \frac{\partial^{2}w}{\partial y^{2}} \qquad . . . 2.1b$$

$$\gamma_{xy} = \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} = -2z \frac{\partial^{2}w}{\partial x \partial y} \qquad . . . 2.1c$$

which are same as for an isotropic case. The deviation from isotropicity shows up only in stress-strain relations which can be written as:

$$\sigma_{x} = \frac{E_{x}}{1 - \nu_{x} \nu_{y}} (\varepsilon_{x} + \nu_{y} \varepsilon_{y})$$

$$\sigma_{y} = \frac{E_{y}}{1 - \nu_{x} \nu_{y}} (\varepsilon_{y} + \nu_{x} \varepsilon_{x})$$

$$\tau_{xy} = \frac{\sqrt{E_{x}E_{y}}}{2(1 + \sqrt{\nu_{x} \nu_{y}})} \gamma_{xy}$$

$$\dots 2.28$$

Potential energy V for a plate is given by

$$V = \frac{1}{2} \iiint_{\tau} (\sigma_{x} \varepsilon_{x} + \sigma_{y} \varepsilon_{y} + \tau_{xy} \gamma_{xy}) d\tau \qquad . . . . 2.3$$

making use of equations (2.1) and (2.2) the above equation reduces to

$$V = \frac{1}{2} \iiint_{\tau} \left[ \frac{E_{x}z^{2}}{(1 - \nu_{x} \nu_{y})} \left( \frac{\partial^{2}w}{\partial x^{2}} + \nu_{y} \frac{\partial^{2}w}{\partial y^{2}} \right) \frac{\partial^{2}w}{\partial x^{2}} \right] + \frac{E_{y}z^{2}}{(1 - \nu_{x} \nu_{y})} \left[ \frac{\partial^{2}w}{\partial y^{2}} + \nu_{x} \frac{\partial^{2}w}{\partial x^{2}} \right] d\tau$$

$$+ \frac{2\sqrt{E_{x}E_{y}}}{1 + \sqrt{\nu_{x} \nu_{y}}} z^{2} \left( \frac{\partial^{2}w}{\partial x \partial y} \right)^{2} d\tau$$

$$= \frac{1}{2} \iiint_{\tau} \left[ \frac{E_{x}z^{2}}{(1 - \nu_{x} \nu_{y})} \left( \frac{\partial^{2}w}{\partial y^{2}} + \nu_{y} \frac{\partial^{2}w}{\partial x^{2}} \right) \frac{\partial^{2}w}{\partial y^{2}} \right] d\tau$$

$$= \frac{1}{2} \iiint_{\tau} \left[ \frac{E_{x}z^{2}}{(1 - \nu_{x} \nu_{y})} \left( \frac{\partial^{2}w}{\partial y^{2}} + \nu_{y} \frac{\partial^{2}w}{\partial x^{2}} \right) \frac{\partial^{2}w}{\partial y^{2}} \right] d\tau$$

Integrating this with respect to z from -h/2 to h/2 we get

$$V = + \frac{h^3}{24} \iint_{A} \left[ D_x \left( \frac{3^2 w}{3^{x^2}} \right)^2 + 2D_x \nu_y \frac{3^2 w}{3^{x^2}} \frac{3^2 w}{3^{y^2}} + D_y \left( \frac{3^2 w}{3^{y^2}} \right)^2 \right] dxdy$$

. . . .2.5

The kinetic energy T of the system is given by

$$T = \frac{1}{2} \iint_{A} \int h(\frac{\partial w}{\partial t})^{2} dxdy \qquad ... 2.6$$

Using the fact that natural modes execute harmonic motion we can write

$$U = T + V = V - \frac{\rho_h \omega^2}{2} \iint W^2 dxdy \qquad ... 2.7$$

$$W = W(x,y) e^{i\omega t} \qquad ... 2.8$$

where

The function  $\mathbb{W}(\mathbf{x},\mathbf{y})$  will be interpolated as beam functions or

$$W(x,y) = \sum_{m} \sum_{n} A_{mn} \emptyset_{m} \left(\frac{\varepsilon_{m} x}{a}\right) \psi_{n} \left(\frac{\eta_{n} y}{b}\right) \dots 2.9$$

where  $\emptyset_m$  and  $\psi_n$  are beam functions in x and y directions respectively.

When W(x,y) as given by equation (2.9) is substituted in equation (2.7), the right hand side becomes function of the co-efficients  $A_{mn}$ . This is minimized by taking the partial derivative with respect to each coefficient and equating to zero. Thus we arrive at a set of equations each of which has the form

$$\frac{\partial V}{\partial A_{ik}} - \frac{\omega^2 f h}{2} \frac{\partial}{\partial A_{ik}} \iint W^2 dxdy = 0 \qquad . . 2.10$$

where  $A_{ik}$  is any one of the coefficients  $A_{mn}$ . Equation (2.10) represents a system of linear homogeneous equations in the unknowns  $A_{mn}$ . The natural frequencies  $\omega_1, \omega_2, \ldots$  are determined from the condition that the determinant of the system must vanish.

#### 2.3 Characteristic Functions for Vibrating Beam:

The different types of beams will be identified by a compound objective which describes the end conditions. Thus a "clamped-clamped" beam is one which is rigidly clamped at both ends; a "clamped-free" beam is clamped at the end x = 0 and free at the end x = 1; a "free-free" beam is free at both ends.

For each type of beam there is an infinite number of normal modes in which the beam can vibrate laterally.

The method of determining the set of characteristic functions which define the normal modes for any type of beam is given in standard references such as (8) and (9). The characteristic functions for the two types of beams used in present work are as follows.

#### Clamped-Free Beam

$$X_{r} = \cosh \frac{\varepsilon_{r} x}{1} - \cos \frac{\varepsilon_{r} x}{1} - \alpha_{r} (\sinh \frac{\varepsilon_{r} x}{1} - \sin \frac{\varepsilon_{r} x}{1})$$

$$r = 1, 2, 3, \dots 2.11$$

#### Free-Free Beam

$$X_{1} = 1$$

$$X_{2} = \sqrt{3}(1 - 2x/1)$$

$$X_{r} = \cosh \frac{\varepsilon_{r} x}{1} + \cos \frac{\varepsilon_{r} x}{1} - \alpha_{r}(\sinh \frac{\varepsilon_{r} x}{1} + \sin \frac{\varepsilon_{r} x}{1})$$

$$(r = 3, 4, 5, ...)$$
2.12a

Each expression defines an infinite set of functions. The numerical values of  $\alpha_r$  and  $\epsilon_r$  for each set of functions are given in appendix.

Tables of values of these functions is given in (10) to five decimal places and at intervals of the argument x/l = 0.02.

Equation (2.12c) is the usual expression for the characteristic functions of a free-free beam, when r=3 we have the first mode of free vibration. The functions  $\mathbf{x}_1$  and  $\mathbf{x}_2$  represent a rigid body translation and rotation and are included in order to obtain a complete orthogonal set.

The boundary conditions satisfied by the functions in each set are the same as the end conditions of the corresponding beam. That is, for the clamped-free functions  $X_r = \frac{dX_r}{dx} = 0$  at x = 0 and  $d^2X_r/(x^2) = d^3X_r/dx^3 = 0$  at x = 1; for the free-free functions

$$\frac{d^2X_r}{dx^2} = \frac{d^3X_r}{dx^3} = 0 \quad \text{at } x = 0 \quad \text{and } x = 1$$

Each of the characteristic functions except those of equations (2.12a) and (2.12b) satisfies the differential equation  $d^4X_r/dx^4 = \epsilon_r^4(X_r/1^4)$ . Each set of the functions is orthogonal in the interval 0 to 1, that is, for any two functions  $X_r$  and  $X_s$  in the same set, the following equations hold

$$\frac{1}{1} \int_{0}^{1} X_{r} X_{s} dx = \delta_{rs}$$

$$\delta_{rs} = 1 \quad \text{for } r = s$$

where 
$$o_{rs} = 1$$
 for  $r = s$ 

$$= 0 for for for for s$$

The second derivatives of the function in each set are also orthogonal and satisfy the relations

$$\int \frac{d^2x}{dx^2} \frac{d^2x}{dx^2} dx = \frac{\varepsilon_r^4}{1^3} \qquad (for r = s)$$

$$= 0 \qquad (for r \neq s) \qquad ... 2.14$$

With the exception of  $X_1$  and  $X_2$  for the free-free functions, equations (2.12a) and (2.12b), for which

$$\int_{0}^{1} \left(\frac{d^{2}X_{1}}{dx^{2}}\right)^{2} dx = \int_{0}^{1} \left(\frac{d^{2}X_{2}}{dx^{2}}\right) dx = 0 \qquad ...2.15$$

In addition to the integrals defined by equations (2.13) and (2.14), it is necessary to evaluate

$$\int_{0}^{1} X_{r} \frac{d^{2}X_{s}}{dx^{2}} dx \quad \text{and} \quad \int_{0}^{1} \frac{dX_{r}}{dx} \frac{dX_{s}}{dx} dx .$$

When using these functions in Raleigh-Ritz method. Values of these integrals have been tabulated in appendix.

Using Equations (2.9) and (2.5), and taking into account the orthogonality relations, equations (2.13) and (2.14), the set of equations (2.10) can be reduced to the form

$$\sum_{m} \sum_{n} \left[ C_{mn}^{(ik)} - \lambda^{2} \delta_{mn} \right] A_{mn} = 0 \qquad ...2.16$$

where

$$C_{mn}^{(ik)} = V_y(E_{mi} F_{kn} + E_{im} F_{nk}) + 2\sqrt{\frac{D_y}{D_x}} (1 - \sqrt{V_x V_y})H_{im}K_{kn}$$
$$+ (\frac{\varepsilon_i^4}{\alpha^2} + \frac{D_y}{D_x} \alpha^2 \eta_k^2) \delta_{mn}$$

$$\lambda^2 = \frac{12 \mathcal{P} \omega^2 a^2 b^2}{h^2 D_x}$$

$$H_{im} = a \int_{0}^{a} \left[ \frac{d \mathcal{Q}_{i}(x)}{dx} \frac{d \mathcal{Q}_{m}(x)}{dx} \right] dx$$

$$K_{kn} = b \int_{0}^{b} \left[ \frac{d\psi_{k}(y)}{dy} \frac{d\psi_{n}(y)}{dy} \right] dy$$

$$E_{im} = a \int_{0}^{a} \left[ \phi_{i}(x) \frac{d^{2} \phi_{m}(x)}{dx^{2}} \right] dx$$

$$F_{kn} = b \int_{0}^{b} \left[ \psi_{k}(y) \frac{d^{2}\psi_{n}(y)}{dx^{2}} \right] dy$$

and  $\varepsilon_i$  and  $\eta_k$  are the eigenvalues associated with the beam modes  $\emptyset_i(\varepsilon_i x/a)$  and  $\psi_k(\eta_k y/b)$  respectively. (Numerical values for the quantaties  $\varepsilon_i$ ,  $\eta_k$ ,  $E_{im}$ ,  $F_{kn}$ ,  $H_{im}$ ,  $K_{kn}$  are tabulated by Young (3) in his paper on isotropic plates and have been reproduced in Appendix II).

#### 2.4 Method for Solution:

There will be one equation for each m.n combination of ik. The characteristic values for  $\lambda$  are found from the condition that determinant of this system of equations must vanish. If there are more than three or four equations in the system, the mathematical labour of expanding the determinant and solving for the roots of the polynomial in  $\lambda$  is prohibitive. In such cases it is expedient to solve for  $\lambda$  by one of the known iterative procedures. One of the advantages of using beam functions is that the diagonal terms in the determinant are large compared to the others and as a result the characteristic values and modes can be found by simple iteration procedure.

For a cantilever plate using 24 term series with m = 1, 2, 3, 4 and n = 1, 2, 3, 4, 5, 6; equation (2.16) gives us 24 equation which can be split up in two groups of 12 equations each. One of these groups include only

n=1, 3, 5 and represent deflections which are symmetrical about the line y=b/2. The other group includes only n=2, 4, 6 and represents deflections which are antisymmetric with respect to the line y=b/2.

For free-free plate the system of equation can be divided into four groups by combination of m and n as odd or even.

Trial vector for  $\mathbf{A}_{mn}$  is chosen and the iterations are carried out till we get convergence to the proper limit.

#### CHAPTER 3

#### PRESENTATION OF RESULTS

#### 3.1 General:

All the results obtained by the present analysis have been tabulated and some of them have been plotted.

The results have been compared with the available ones wherever it was possible and the interpretation of the results has been carried out.

#### 3.2 Comparison of Results:

In the present work calculations were carried out for five different materials out of which one falls in the category of isotropic materials. The properties of different materials which were selected for the present work are given in Table 3.2.1.

Nature of material	E <sub>x</sub> (Ksc)	Ey (Ksc)	$v_{x}$	$\lor_{ m y}$	Ey/Ex
Plywood	1x10 <sup>5</sup>	0.5x10 <sup>5</sup>	0.05	0.025	0.5
Plywood	1x10 <sup>5</sup>	0.05x10 <sup>5</sup>	0.2	0.01	0.05
Epoxy resin	2.8x10 <sup>5</sup>	0.224x10 <sup>6</sup>	0.2	0.016	0.08
Graphite-epoxy			0.24	0.0165	0.06875
Isotropic			0.3	0.3	1.0

TABLE 3.2.1

Table 3.2.2 compares the values for frequency parameter obtained by Young (3) for square cantilever isotropic plate with the values obtained by present analysis.

$\frac{\omega}{\sqrt{D/\text{fha}^4}}$	1 <sup>st</sup> mode	2 <sup>nd</sup> mode	3 <sup>rd</sup> mode	4 <sup>th</sup> mode	5 <sup>th</sup> mode
Young	3.494	8.547	21.44	27.46	31.17
Present yalues	3.4937	8.5441	21.44	27.4562	31.17

TABLE 3.2.2

The values were obtained by taking 18 terms in equation (2.16). As can be seen from the table the values obtained by present analysis are in excellent agreement with the values obtained by Young (3).

Barton (11) calculated the values of frequency parameter  $\lambda$  (=  $\frac{\omega}{\sqrt{D/\rho_{\rm ha}4}}$ ) of an isotropic plate with different aspect ratios (=  $\frac{a}{b}$ ; a > b). These values are tabulated in Table 3.2.3. Comparing these values with the values obtained by present analysis, given in Table 3.2.4 after changing  $\lambda$  to  $\bar{\lambda}$ , we find that the values are same except in second mode in which present values are slightly lower.

 $\overline{\lambda}$  Obtained by Barton for Isotropic Cantilever Plate

a/b		Mc	de Numbers	3	
a/ U	1.	2	3	4	5
0.5	3.508	5.372	21.96	10.26	24.85
1.0	3.494	8.547	21.44	27.46	31.17
2.0	3.472	14.93	21.61	94.49	48.71
5.0	3.45	34.73	21.52	563.9	105.9

TABLE 3.2.3

 $\overline{\lambda}$ Obtained by Present Analysis for Isotropic Cantilever Plate

- /1	Mode Numbers				
a/b	1	2	3	4	5
0.5	3.508	5.372	21.96	10.26	24.85
1.0	3 • 494	8.544	21.44	27.46	31.17
2.0	3.472	14.92	21.61	94.48	48.71
5.0	3.45	34.71	21.52	563.9	105.9

TABLE 3.2.4

Table 3.2.5 compares the results given by Basily and Dickson (7) and Mohan and Kingsbury (6). Present values are higher than the values given by both of them. It is because Mohan and Kingsbury used Galerkins method without modifying it for the free edges whereas Basely and Dickson used Ritz method but their frequency equation is wrong as has been pointed out earlier.

 $\lambda$  for Cantilever Orthotropic Plate  $E_y/E_x = 0.06875$  and  $v_x = 0.24$ 

		Basily & Dickson (Ritz)		Mohan & Kingsbury	Present Analysis (Raleigh-Ritz)	
r	<b>S</b>	4x4	4x5	Galerkin (4x4)	5x6	
0	0	3.514	3.515	3.516	3.5157	
0	1	4.191	4.191	3.516	5.9016	
0	2	8.205	8.181	6.5	11.3686	
0	3	17.76	17.75	16.4	21.0445	
1	0	22.03	22.03	22.03	22.03	
1	2	26.14	25.96	23.1	34.3139	
1	1	22.87	22.87	22.03	25.4860	
0	4		32.98		34.3149	
1	3	33.34	33.33	28.6	47.0021	

TABLE 3.2.5

#### 3.3 Summary and Conclusions:

All the results have been tabulated and are presented. Figures have been drawn to bring out the dependence of frequency parameter on different plate parameters.

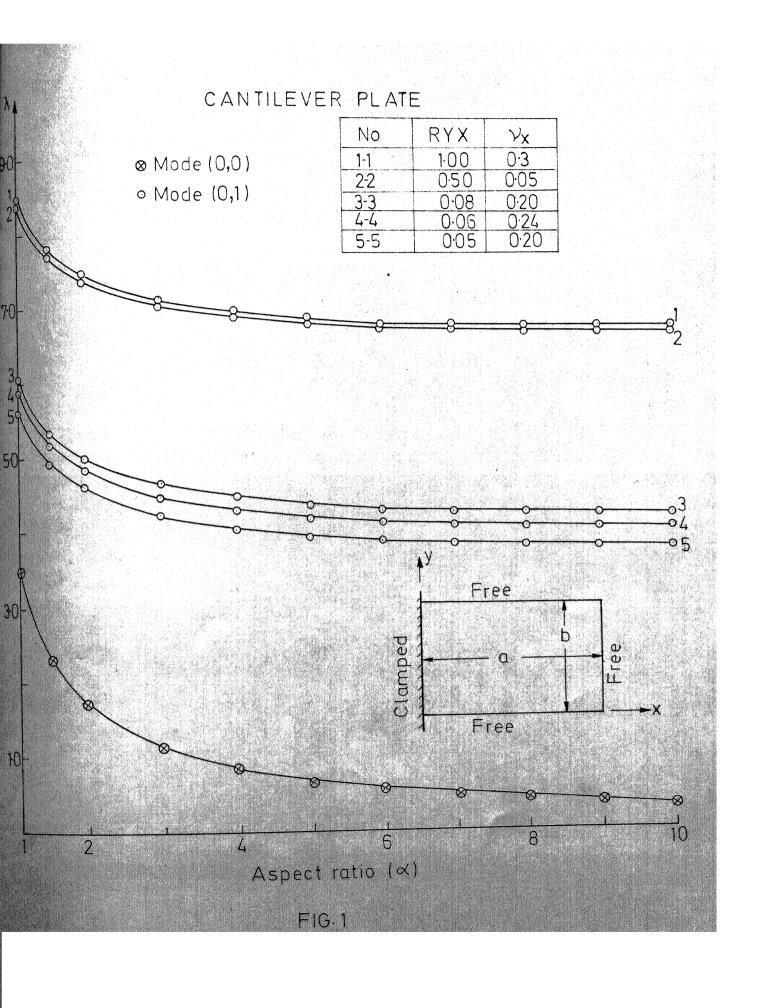
#### 3.3.1 Convergence of Rayleigh-Ritz Method

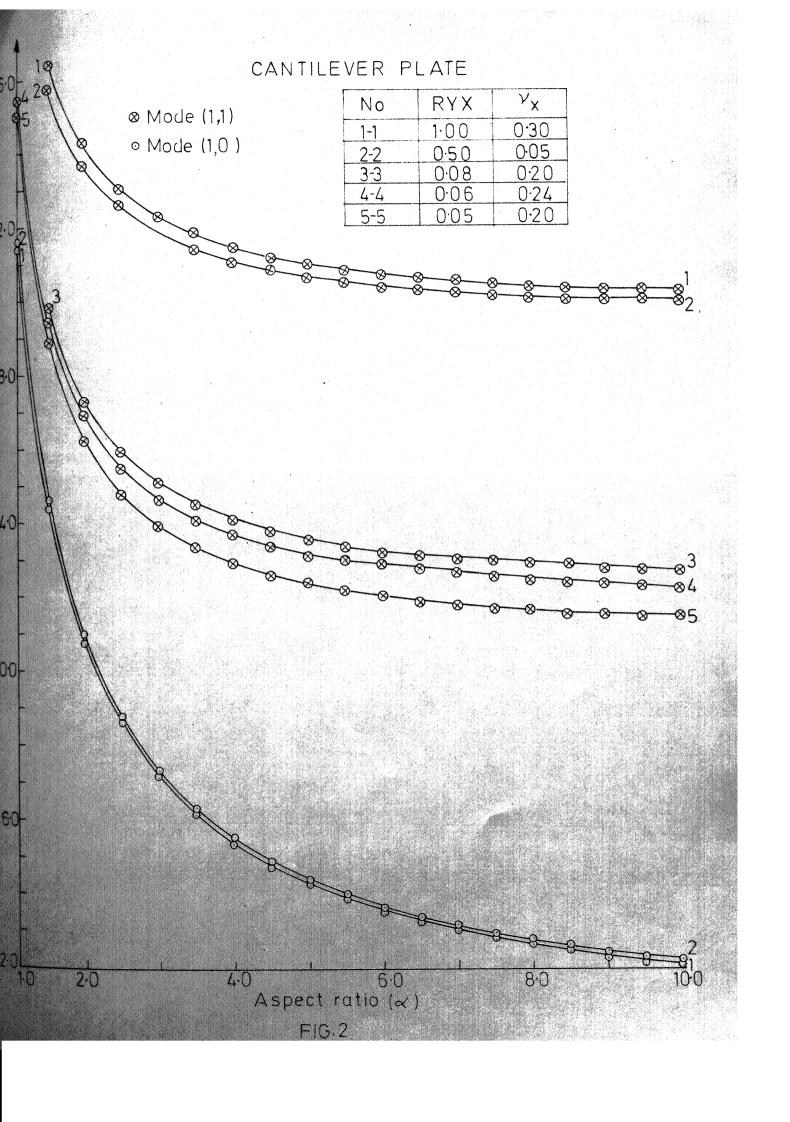
Calculations were carried out with 18 (T. Nos. 1.00, 1.10, 1.20 and 1.30), 24 (T. Nos. 1.01, 1.11, 1.21 and 1.31), 30 (T. Nos. 1.02, 1.12, 1.22 and 1.32) number of terms in the interpolating function. The convergence of Rayleigh-Ritz method with respect to number of terms in the interpolating function is very good as can be observed by comparing the above said tables.

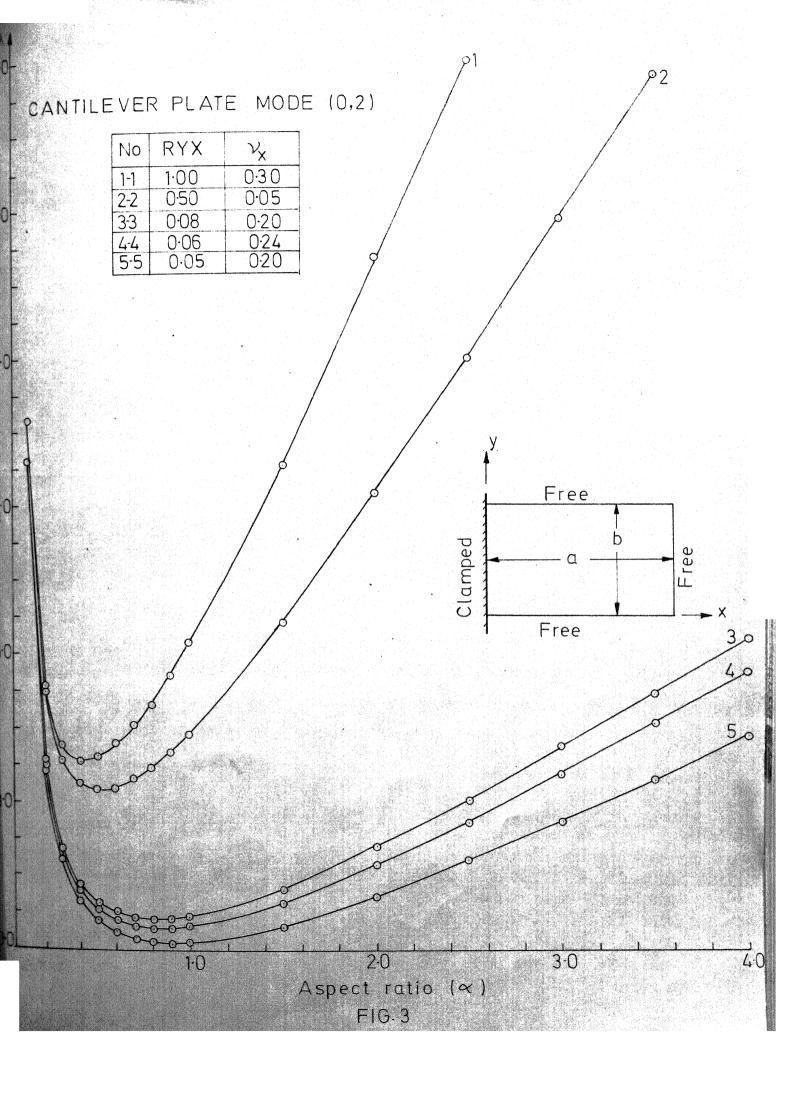
Convergence of Rayleigh-Ritz method is fairly good except for certain frequencies which did not converge even after iterating them for half an hour on 7044 computer. The frequencies which did not converge were:

T. No. Mode		Aspect ratio
2.00	(1,1)	0.60
2.20	(1,0)	0.90
2.30	(1,1)	0,30

TABLE 3.3.1





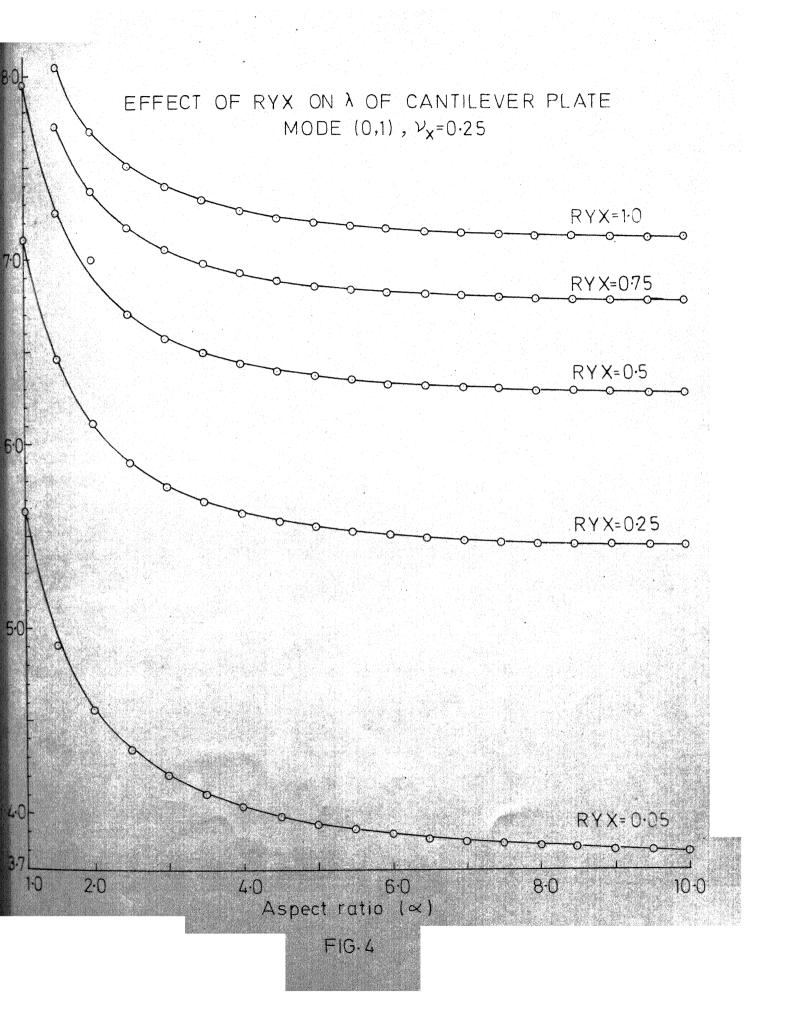


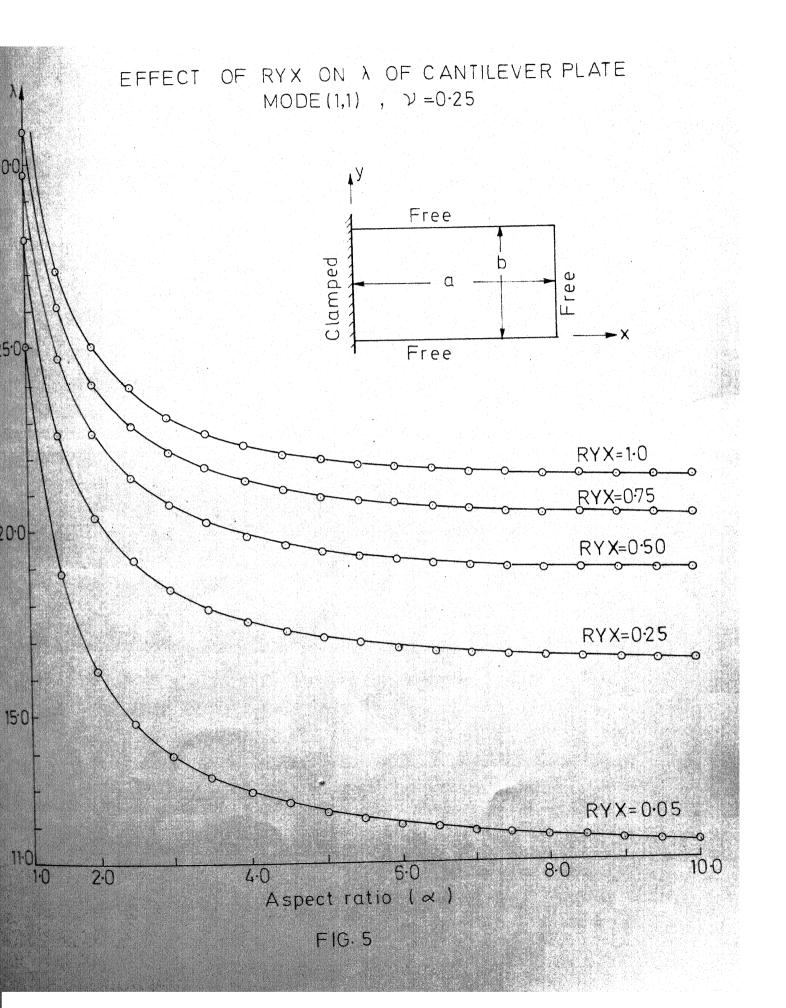
It seems that after few it erations either the convergence rate becomes poor or the iterations itself start oscillating.

## 3.3.2 Effect of Aspect Ratio on Frequency Parameters

Frequency parameter  $\nearrow$  decreases for modes (0,0), (0,1), (1,0) and (1,1) for increasing aspect ratio (Figs. 1 and 2). The rate of decrease for the first two modes is lower than the other two. The decrease in the frequency parameter should be expected as the aspect ratio increases because the effective stiffness of the plate decreases.

For mode (0,2) it shows a minimum and hence increases after some point as aspect ratio increases (Fig. 3). This increase is not in any case contradicting to the statement given earlier because decrease in frequency does not necessarily mean a decrease in frequency parameter. Frequency parameter is itself a function of aspect ratio and hence an increase imaspect ratio and decrease in frequency can result iman increase in the frequency parameter. If we change the frequency parameter from  $\lambda^2 = 12 \int_0^{\infty} \lambda^2 a^2 b^2 / h^2 D_x$  to  $\lambda^2 = 12 \int_0^{\infty} \lambda^2 b^4 / h^2 D_x$  then the frequency parameter shows a decreasing trend as is shown in Table 3.3.2.





Aspect ratio	1.00	2.00	5.00	10.00
$\overline{\lambda}$	10.5042	6.4844	5.2397	5.0618

TABLE 3.3.2

Here increase in aspect ratio and decrease in frequency parameter can be interpreted as increase in dimension a i.e. length of cantilever side, decreases frequency which is expected.

# 3.3.3 Effect of $E_y/E_x$ on frequency parameter

Referring to Figs. 4 and 5 it can be seen that increase in RYX (=  $\rm E_y/E_x$ ) brings about an increase in frequency parameter, as should be expected, for antisymmetric modes. For symmetric modes the frequency parameter does not show significant dependence on RYX as can be seen from Tables 4.00 and 4.20.

#### 3.3.4 Effect of Poissons Ratio on frequency parameter

For symmetrical modes frequency parameter is practically independent of poistons ratio, as can be observed from Tables 3.00 and 3.20. The maximum change being 0.2%.

For antisymmetric modes the frequency parameter changes merely by 4% (maximum). See Tables 3.10 and 3.30.

#### 3.3.5 Discussion on Free Plate

Frequency parameter  $\lambda$  has been calculated for first five modes of the material with  $E_y/E_x=0.06875$  and Poissions ratio = 0.24 (Table 5.0).

First three modes have zero frequencies and these represent rigid body translation and rigid body rotation about x = a/2 and y = b/2 line.

Mode (1,1) shows a minimum whereas mode (2,2) increases steadily which is not unexpected because if  $\lambda$  is changed to  $\overline{\lambda}$ , both these modes show a decreasing trend.

Referring to design tables for free plate one can observe that effect of RYX is pronounced. As RYX increases  $\lambda$  also increases and the effect of poistons ratio on  $\lambda$  also becomes significant.

#### .4 Scope for Further Research:

Following areas can be explored further.

Use of Generalized Galerkins approach to solve such problems would give more insight even though it may involve great amount of computational labour.

- 2. Convergence rate of Raleigh-Ritz method may be studied to investigate the convergence of such frequency parameters as given in Table 3.3.1.
- 3. Effect of non-linear vibrations on the frequency parameter can be studied.
- 4. Vibrations of orthotropic plates with other boundary conditions can be studied.

#### REFERENCES

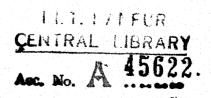
- 1. Laura, P.A. and Bernard, F. Saffell, Jr. 1966
  J. of Acoustical Society of America 41, 836. Study
  of small amplitude vibration of clamped rectangular
  plates using polynomial approximations.
- 2. Maurizi, M.J. and Laura, P.A. 1973 J. of Sound and Vibration 26, 299. Vibration analysis of clamped rectangular plates of generalized orthotropy.
- 3. D. Young 1950 J. Appl. Mech. 17, 448. Vibration of rectangular plates by Ritz method.
- 4. J.E. Ashton and J.D. Anderson 1969 Shock and Vibration Bulletin 39, 81-91. Natural modes of vibration of boron-epoxy plates.
- 5. J.E. Ashton 1969 Shock and Vibration Bulletin 39, 93-100. Natural modes of free-free anisotropic plates.
- 6. D. Mohan and H.B. Kingsbury 1971 J. of Acoustical Society of America 50, 266. Free vibration of generally orthotropic plates.
- 7. S.F. Bassily and S.M. Dickson 1972 J. of Accoustical Society of America 52, 1050. Comments on "Free Vibration of Generally Orthotropic plates" by D. Mohan and H.B. Kingsbury.
- 8. "Theory of Sound" by Lord Rayleigh, Second American edition, Dover Publications, New York, N.Y. 1945.

- 9. "Vibration Problems in Engineering" by S. Timoshenko, Second edition, D. Van Nostrand Company Inc., New York, N.Y. 1937.
- 10. "Tables of Characteristic Functions Representing the Normal Modes of Vibration of a Beam" by D. Young and R.F. Flegar, Engineering Research Series, No. 44, University of Texas, Austin, Texas.
- 11. M.V. Barton 1951 J. Appl. Mech. Trans. ASME 73, 129.

  Vibration of rectangular and skew plates.
- 12. R.F. Hearmon 1952 J. Appl. Mech. 19, 402. The frequency of vibration of rectangular isotropic plates.
- 13. A. Weinstein 1951 J. Appl. Mech. 18, 229. Discussion of vibration of rectangular plates by Ritz method.
- 14. N.J. Huffington, Jr. and W.H. Hoppmann II 1958

  J. Appl. Mech. 25, 389. On the transverse vibration of rectangular orthotropic plates.
- 15. J.E. Ashton 1969 J. Composite Materials 3, 470.

  Analysis of anisotropic plates.
- 16. Leonard Meirovitch Analytical Methods in Vibration,
  McMillan
- 17. An Introduction to Applied Anisotropic Elasticity R.F. Hearmon, Oxford University Press, 1961.
- 18. A First Course in Numerical Analysis Anthony Ralson, McGraw Hill Book Company, 1965.



### APPSNDIX-I

AEGICA, TIMEDOB, PAGESOOS, NAME INDER KRISHEN PANDITTA I. GLO 18 TC. <del>\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\*\*\*\*</del> \* THIS PROGRAMM CAN SVALUATE SIGNVALUES AND MIGNVECTORS OF A PLST \* WITH ANY COMBINATION OF CANTILEVER AND FROM FROM OBGOS. \* NAR -NUMBER OF ASPECT RATIOS FOR WHICH RESULT IS THE DECLARACTED RATED STARTS FROM 1.0 AND IS INCREMENTED BY DELAR. NESAS-EFFECTIVE SYMMTRY ANTISYMMTRY. =NUMBER OF TERMS IN K-DIRECTION. =NUMBER OF TERMS IN Y-DIRECTIOM. \* NEX = NUMBER OF EFFECTIVE TERMS IN K-DIRECTION. =NUMBER OF EFFECTIVE TERMS IN Y-DIRECTION. 2 \* NEY \* NMAT = NUMBER OF MATERIALS FOR WHICH RESULT IS METERDED. =NUMBER OF MODAL FREQUENCIES. \* NMF \* NSME = NUMBER OF MODAL FREQUENCY FROM WHICH YOU WART TO START. \* NJMF = INTERVAL IN THE MODAL FREQUENCIES. =ASPECT RATIO. \* AP FRATIO OF Y-DIRECTIONAL YOUNG&S MODULAS, YOUN-DIRECTIONAL YOUNG&S RYX 1 MODULAS. \* PX =POISON&S RATIO IN X-DIRECTION. =POISON&S RATIO IN Y-DIRECTIOM. \* DY =ACCURACY FOR CIGNVALUES AND TIGNVECTORS. \* ICONV =MAXIMUM ITTERATIONS ALLOWED FOR CONVERGENCE. 25 NSASY=1 AND 2 NJY=2 25 X-SYMMTRY K=YUM S BUA J=YBAZM Y-SYMMTRY NSASK=1 MJ/ = 1 IF THERE IS NO SYMMTRY MSASY=1 1.JY= AND <del>\*</del> DIMENSIONA (20), AA (20), B (20, 20), C (20, 20), D (20, 20), C (20, 20), EX (20); 18Y(20),F(20,20),H(20,20),SMM(20),RYX(20);PX(16),PY(16) READ 90, ((E(I,J),I=2,5),J=3,5)READ 90, ((H(I,J), I=1, 5), J=1, 5)READ 90, ((B(I,J),I=1,7),J=1,7)READ 90, ((F(I,J), I=1,7), J=1,7) READ 90, (EX(I), I=1.5)

READ 90, (EY(I), I=1,7)

READ 90, EP

```
READ 992, NAR, NESAS, NX, NY, NEY, NEY, NMAT, ICONV
    READ 990 , NSMF , NMF , NJMF
    READ .93, (RYX(I), PX(I), I=), NMAT), DELAR
    FORMAT(%QI2)
    FORMAT (2835.8)
    FORMAT (8(FE0.5))
    DO 991 III=1, NESAS
    READ 992 + NSASX + NSASY + NJX + NJY
    PRINT 6, NSMF, NMF, NJMF
   FORMAT(//30%, *THE MODAL FREQUENCIES CALCULATED BELOW ARE FROM NO. *
1, 12, * TO NO. *, 12, * IN STEPS OF*, 12//)
    PRINT 5. NSASX, NSASY, NJX, NJY, NY
    FORMAT(SOX,*ADAACH*,12,100X,*ADAACH*,12,100X,*ADAACH*,12,100X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,110X,*ADAACH*,1
112,10 X,*NX=*, 12,10X,*NY=*,12///)
    DO 999 IMAT= S, NMAT
    PY(IMAT)=PX(IMAT)*RYX(IMAT)
    PRINT 95, RYX(IMAT), PX(IMAT)
    FORMAT(55X,60(3H*)/43X,*RYX=*,255,8,00X,*FX=*,355,8,6/57,000(3H*)/
    AR=0.1
    DO 770 IAR = ... NAR
    PRINT 772, AR
    FORMAT(SOX,*THE FOLLOWING ARE THE RESULTS FORMA CANTILOVER PLATE
1F ASPECT RATIO=*, F6.2)
   FROM HERE CALCULATION FOR NAY BY MAY MATRIX, USING BEAM-FUNTIONS, STARTS.
    J=1
    NU SUN TENSAS NE NO SUN DO SUN
    DO 200 K=NSASY, NY, NJY
   L=1
   XLM.XXASX=M 00% DD
   PU 100 N=NSASY, NY, NJY
   IF(M. EQ. I. AND. N. EQ. K)
                                                                                                         GO TO 10
    GC TO 120
    C(M,N)=PY(IMAT)*(E(M,I)*F(K,N)+E(I,M)*F(N,K))+2.*SCRT(RYE(IMAT))*
1(1.-SQRT(PX(INAT)*PY(IMAT)))*H(I,M)*B(K,N)+(EX(I)**A)/AR** +(EY(K)
2**4)* (AR**2)*RYX(IMAT)
   GO TO 101
   C(M, V) = PY(IMAT) *(E(M, I) *F(K, N) +E(I, M) *F(N, K)) +2, *SQRT(RYA(IMAT)) *
1(1.-SQRT(PX(IMAT)*PY(IMAT)))*H(I, M)*B(K, N)
```

```
D(J,L)=C(M,N)
L=L+1
J=J+ .
NXY=VEX*NEY
DO 300 I=1,NXY
Y N . 1=L OCE OC
C(I,J)=D(I,J)
FROM HERE CALCULATIONS FOR EIGNVALUES AND BIGHVECTORS START.
DO 608 NE=NSMF, NMF, NJMF
W=0.0
FF=0.0
DO 402 J=1,NXY
C. C= (L) AA
A(J) = 0.0
A(NF) =1 . 0
AA(NF) = .0
IJ=1
CONTINUE
DO 500 I=1, NKY
SuM=D.O
DB 400 J=1, NKY
IF(I.EQ.J) GO TO 9%
GO TO 92
CONTI NUE
IF(I. EQ.NF.AND.J.EQ.NF) GO TO 92
GC T3 400
SUM=SUM-C(I,J)*A(J)
CONTI NUE
IF(I. EQ. NF) GO TO 403
GC TO 40)
W=-SJM
GO TO 500
A(I) = SUM/(C(I,I)-W)
CONTI NUE
DO 600 J=1,NXY
IF(ABS((A(J)-AA(J))/A(J)).LE.EP.AND.ABS((W-FF)/W).LE.PP) GO TO ON
DC 602 I=1,NXY
AA(I) = A(I)
FF=W
I J = I J + 1
IF(IJ.GT.ICONV) GD TD 600
GO TO 603
CONTI NUE
WW=W* *0.5
PRINT 700, WW, (A(K), K=1,8), IJ, (A(K), K=9, MXY)
FORMAT(/1X,9F14.4/7X,13,5X,8F14.4)
PRINT 505
```

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FORMAT(2X, 322(3H*))
FORMAT(LX, 180(1H-)/3X = 180(1H*)/1X, 180(1H-)/)
 CONTINUE
 PRINT 505
 AR=AR+DELAR
FORMAT(//3%, 350(SH*)//50%, *CALCULATION FOR MOW MATERIAL*// G. SUNE
5H*1/1
 CONTI NUE
 CONTI NUE
 STOP
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                            2.08737 0.91404 -28.74828 -28.8942 0.3293
-9.04222 -25.90423 - 4.25863 -20.2828 -27.8908
4.78605 -88.98662 -88.70938 08.78608 -7.88893
RY
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                   9.85075
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NUMBER OF TERMS IN SERIES=18

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2.50 *		4.5707	8.8863	34.8828	14.8275	- 16 - 16
5.CC	4.2718	* Z 3	7.3420	16.9854	38.9809	
3.50	3.0C4A	4.1283	£.2552	19.23.47	12.4125	教
4.00 *	0.8788	4.0581	5.5064	21.4960	22.9957	*
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5.00	c.7030	9661	4.405%	26.3984	12.4575	
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7.00	0.5021	8783	3.1464	35.8638	11.9041	
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8.50	C.4135	3.8421	2.591.	43.7184	11.6909	) # ·
9.00	0.3905	3.8343	2.4471	45.6811	11.6398	*
5.50	C.3700	3.8277	2.3183	46.1478	11.5957	
10.00	C.3515	3.8219	2.2024	50.6180	11.5574	
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NUMBER OF TERMS IN SHRIES = 24

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TIO	* (C,O) *	(O, I)	(), , ()	(0,8)	<b>3</b> 4
1.00		5.6546	22.0328	10.4810	26.0413 *
1.50	* 2.3438	4.9199	14.6910	11.3497	* \$5.9078 * *
2.00	* * 1. <b>7</b> 578	4.5653	11.0101	32.5300	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1
2.5C	* * 2.4067	4.3508	E.8763	14.8419	* \$4.8845 *
3.00	* * 1.1718	4.2071	7.3420	16.9461	* - 3.5.95% * *
3.50	* * 1.0043	4.1050	6.2931	19.1763	13.3882 *
4.00	* * C•8788	4.0319	5.5064	21.4587	* *2.974* *
4.50	* C.7811	3.9760	4.8945	23.7921	72.671A *
5.00	* * C.7630	2.9314	4.4050	26.702	12.43 54 *
5.50	* * 0.6392	3.8958	4.0045	28.560	* 25.25.27
6.00 3	* * C.5858	3.8692	3.6707	30.9752	* 12.1096 *
6.5C	* * C.5407	2.8462	3.3883	33.4015	9900 *
7.00	* * 0.5021	3.8309	3.1403	35.8484	* 11.8912 *
7.50		3.8156	2.9365	28.2940	
8.00	* C.4393	2.8027	2.7529	40.7466	
8.50		5.7938	2.5910	43.2051	11.7153 *
9.00	* C.3905	<b>⇒.7824</b>	2.4470	45.6683	
9.50	* C.3699	3.7743	2.3182	48.1357	11.6264 *
0.00	* 0.3514	3.7673	2.2023	50.6064	* 11.5908 *

RYX = 0.05CCC PEISIENS RATIO = 0.20

NUMBER OF TERMS IN SERIES = 30

ASPECT	1 225 COM	nata ning nata ning ning ning ning ning ning ning nin	MCDES		
RATIO		(0,1)		(O+2)	# #
PALL :					*
1.00	<b>3.515</b> 9		22.0328	10.4823	25.0360 *
1.50	2.3438	4.9199	14.6910	11.3505	18.8940 <b>*</b>
2.00	1.7578	4.5655	11.0101	12.9291	16.2128 *
2.5C	1.4062	4.3509	8.8103	14.8393	14.7768 *
3.00	1.1718	4-2074	7.3420	16.9400	13.9013
3.50	1.0043	4.1058	6.2931	19.1686	13.3160
4.00	0.8788	4.0311	5.5064	21.4498	12.8986
4.50	0.7811	3.9743	4.8945	23.7825	12.5871
5.CC	0.7030	3.9300	4.4050	26.1631	12.3470
5.50	0.6391	3.8947	4.0045	28-5521	12.1574
_6.00	0.5858	3.8661	3.6707	30-9548	12.0047
6.50	0.5407	3.8426	3.3883	33.3977	11.8798
7.0C	0.5021	3.8231	3.1463	35.8318	11.7764
7.5C	0.4686	3.8066	2.9365	38.2773	11.6897
8.00	0.4393	3.7926	2.7529	40.7304	11.6163
8.50	0.4135	3.7805	2.5910	43.1893	11.5537
	0.3905	3.7702	2.4470	45.6531	11-4998
	0.3699	3.7611	2.3182	48.1209	11.4532
10.00	* 0.3514	3.7533	2.2032	50.5922	11.4125
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RYX = 0.06875 POISIONS RATIC= 0.24

NUMBER OF TERMS IN SERIES=18

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* 3.00 * 1.1715 4.4895 7.3393 19.5210 14.71	20 *
* 3.50 * 01.0041 4.3937 6.2907 22.2097 14.15	* 8.
* 4.00 * 0.8786 4.3244 5.5042 24.9276 13.75 *	15 *
* 4.50 * 0.7809 4.2725 4.8925 27.6961 13.45 *	*
5.00 * 0.7028 4.2335 4.4031 30.4981 13.22	*
5.50 * 0.6389 4.2032 4.0028 33.3242 13.04	*
* 6.50 * 0.5856 4.1794 3.6691 36.1684 12.89 * 6.50 * 0.5406 4.1602 3.3869 39.0263 12.77	*
7.00 * 0.5019 4.1447 3.1449 41.8951 12.68	*
* 7.50 * 0.4685 4.1319 2.9352 44.7725 12.60	* 21 * *
*	
* 8.50 * 0.4135 4.1108 2.5898 50.5471 12.47	766 * *
* 9.00 * 0.3904 4.1034 2.4459 53.4420 12.42	273 *
* 9.50 * 0.3698 4.0971 2.3172 56.3410 12.38 * *	*
* 10.00 * 0.3513 4.0916 2.2013 59.2435 12.34 *	481 * *

RYA = C.CS878 PCISICNS RATIE = 0.24

NUMBER OF TERMS IN SERIES = 24

		A R. O. F. C. B. S. P. S. S. B. B. C. B. C.	BADE O BOTE O EST BODE BOYEST BOY 2	Pitropul kinopulatu pro pitropulatin pitrop Programa	en della della La compositoria della
ASPECT *			<b>PCCES</b>		性
RATIC *	(0,0)	(0,2)	(X,C)	(0,%)	(1,1) *
Harris Com No.	i de l'articació de trado de la detración de la del	to konkul kuloku konkonko konkonko	CD 4 - ARTHUR PORTORIA CONCOR	en e	S. W. Street and Land Control March
4					*
	3.5157	5.9019	22.0219	24.8689	25.4895 *
2.5C ×	2.3426	5.1770	6.6115	12.6115	19.4863 *
Z.CC *	.7575	4.8213	11.CC65	14.6222	16.9C09 *
2.5C *	1.4059	4.6055	€. EC7C	16.9645	15.5256 *
3.00	1.1715	4.4621	7.3392	19.4779	14.6881 *
3.5C.	2.0042	4.3617	6.2906	22.1658	14.1266 *
4.00 *	C.8785	4.2886	5.5641	24.8826	13.7328 *
4.5C *	C.7809	4.2334	4.8924	27.6955	13.4437 *
5.CC *	0.7028	4.1894	4.4030	30.4673	13.2C53 *
5.5C *	C.6388	4.1556	4.0026	33.2932	13.C262 *
6.00 *	C.5856	4.1284	3.6690	36.1283	12.8829 *
6.5C *	C.5404	4.1063	3.3867	38.9975	12.766: *
7.05	0.5019	4.0923	3.1447	41.8676	\$2.7C\$2 *
7.50 *	0.4984	4.077€	2.935C	44.7464	12.6249 *
e.oc *	0.489%	4.0652	2.7515	47.6320	12.561 *
8.3C *	C.40.28	4.0492	2.5857	50.334	12.5072 *
9.00 *	<b>C.</b> 3900	4.0399	2.4658	51.4195	12.4614 *
9.5C *	C.3698	4.0319	2.8170	56.3195	12.4220 #
1 1C.GC *	C.2313				2.3880 ×

TABLE NC .= 2.5

PYA = 0.05875 PEISIENS RATIC = 0.24

NUMBER OF TERMS IN SERIES = 30

general encountries	in a ca encare por la successia.	(2) 動作動力 取分量性 電視 2世 概以更多	entre militari i entre militari entre e	a two creek received as	nama an anaman an an an an an a
ASPECT			MCCES		
FATIC #	(0,0)	(0,%)	( * · C )	(0,8)	(2,3)
A STATE OF S	i Çiroleriye zasılık veziyetine İev ayıla T	n den karakan kan kan den karakan karakan kan den kan den kara	機(24年) 「神・神) (東) (東75 春) (東05 年 下東) (Pr	ado mado prio e acor vide de la dada pres e	響。 Cal almonation and a feet 編
1.00 *	5.53.57	5.901€	22.0319	33686	25.4860 *
1 2 . X C N	'	5.1769	6.61.06	12.6106	*9.4698 *
# 2.0C #		4.8215		14.6198	16.8657 *
2.5C	.4059	4.6058	8.EC7C	16.9605	15.4780 *
* 0.00 *	1.1735	4.4622	7.2392	19.4726	14.6246 %
9.5C +	1.004	4.3672	6.2904	22.1593	24.CF28 *
4.00		4.2870	5.504	24.8752	13.6378
4.5C	C.7808	4.2309	4.8924	27.6874	13.328) *
5.CC	C.7027	4.1873	4.4030	30.4573	12.0890 *
5.5C	C.6388	4.1527	4.0026	33.2757	12.8998 *
6.00	C.5856	4.1247	3.6690	36.1434	12.7467 *
A.BC		4.1017	3.3867	38.995	12.6215 *
7.00	0.5019	4.0826	3.1447	41.8639	12.55C3 #
7.00	€ 0.4689	4.0666	2.9350	44.7421	12.4669 *
* 8.UC	r C.4391	4.0530	2.7515	47.6276	12.3966 *
• 8.5¢ ·	\$ 0.42.23	4.0413	2.5896	50. 589	12.3369 *
	* 0.3903	4.0313	2.4457	53.415C	12.2857 *
	* 0.3698	m.0226	2.3170	56. 151	
. 1C.CC	c.3513	4.0150	2.2011	59.2186	12.2031 *
	· Proposition	து வது தகையுக்கு வெள்ளுக்கும். இது தகையுக்கு வெள்ளுக்கும்.		or morning someon	

PYNE C.SCOCS PEISIENS RATICE 0.65

NUMBER OF TERMS IN SERIES=18

BERT TERM OF FOR	us - maka kushuskan katik kati M	#m.#iv.kupfins.#us#ndings#ig.#kg	្នា ភូឌ្ឍាស់ «សេសស្គាល់» ព្រៀបប្រៀ ព្រ	A BELORAL RUPOVETO	ន"…ស់ទី២០១៩ ១៩១១២៣០២៣៤០៤ តែបាន -	. :
ASPECT	* *		MCCES			※
	* (C,C)	(0,3)	( ] , C )	(0, %)	(1,1)	4 4
Market W. C. R. P.	Non troplar of his entropies.	A	Sault nerzyczec au amponac	LANGUAGE CONTRACTOR	en entretari en neuro en escribir quar	*
	8 3.5158	8.4067	21.8164	21.6875	30.6624	棒棒棒棒
2.50	2.3438	7.7078	4.6862	27.7178	25.864	ĸ
	.7578	7.3548	11.C146	34.6349	22.8149	影響
ľ	× 1.4362	7.1629	8.8316	42.940	22.6993	替被
2.cc	* 1.2718	7.0535	7.3429	49.4485	22.CC67	型 火 香
3.5C	% 3.CC44	5.9750	6.2938	57.0733	25.5440	4
	* C.8788	6.9175	5.5C71	64.7697	21.2196	≫ - - 
4.5C	* c.7812	6.8805	4.895	72.5138	20.9836	· ·
	* C.7030	6.8533	4.4056	80.3512	20.807	4
5.5C	* C.639%	6.8328	4.005	88.0929	20.6718	传教
6.0C	C.5859	6.8170	3.6713	95.9126	20.5659	林
	c.5408	6.8258	3.3889	103.7464	20.4816	中
7	0.5022	0.7945	3.1468	111.5910	2C.4195	育
7	2.4687	6.7864	2.9370	119.4444	20.4384	装置
Ş	4 0.4394	6.7797	2.7534	27.3049	20.3965	*
	C.4233	6.7741	2.5915	35.1712	20.3616	**
7.00	* C.3906	5.7694	2.4475	143.0424	20.3322	整
<b>1</b>	c.3700	6.7655	2.3187	,5C.9178	20.3072	景景
* * 10.00		6.7620	2.2027	58.7966	20.2858	報
	<b>₩</b>			Market Live Live	The second secon	7.

RYX = 0.50000 POISIONS RATIC = 0.05 NUMBER OF TERMS IN SERIES=24

PECT *			MCDES		
* * DITA *	(0,0)	(0,1)	(1,0)	(0,2)	(2,1)
* *	3.5158	8.3825	21.7346	21.6539	30.6397
* 1.5C *	2.3437	7.6688	14.6897	27.6244	25.8226
* 2.00 *	1.7580	7.3139	11.0173	34.5432	23.7797
* 2.5C *	1.4060	7.1099	8.8138	41.8607	22.6637
* 3.00 *	1.1720	6.9788	7.3449	49.3787	23.9762
* 3.50 *	1.0046	6.8966	6.2956	57.0105	21.51.79
<b>*</b> 4.00 *	0.8790	6.8367	5.5086	64.7130	21.1567
* 4.50 *	0.7813	6.7933	4.8966	72.4572	21.0210
. * 5.00 *	0.7032	6.7608	4.4069	80-2583	20.8596
# 5.50 *	0.6393	6.7960	4.0063	88.0496	20.7297
6.00 ×	0.5860	6.7165	3.6724	95.8727	20.6318
* 6.50 *	0.5409	6.6898	3.3899	103.7092	20.5544
7.00 *	0.5023	0.6757	3.1478	111.5564	20.4921
* 7.50 *	0.4688	6.6633	2.9374	119.4120	20.4413
* 8.0C *	0.4395	6.6570	2.7543	127.2745	20.3994
	0.4136	6.6466	2.5923	135.1395	20.364
* 9.00 *		6.6432	2.4483	143.0118	20.299
* * 9_50 *	0.3701	6.6515	2.3194	150.8921	20.273
10.00 ×	0.3516	6.6471	2.2035	158.7722	20.251

NUMBER OF TERMS IN SERIES=30

* SPECT *			MCDES		**
* * ATIO * *	(0,0)	(0,1)	(1,0)	(0,7)	(
1.00 *	3.5158	8.3827	21.6272	21.6272	30.6032
* %.50 *	2.3437	7.6659	14.6861	27.6380	25.7427
* 2.0C *	1.7577	7.3136	11.0146	34.5551	23.6550
2.5C *	1.406	7.1070	8.8115	41.8577	22.5128
* 3.00 *	1.1718	6.9754	7.3428	49.2779	21.8022
3.50 *	1.0043	6.8859	6.2938	56.8865	21.3256
* 4.00 *	C.8788	6.8222	5.5070	64.7192	20.9892
4.50 *	0.7811	6.7751	4.8950	72.4604	20.7430
5.00 *	0.7030	6.7393	4.4055	80.2416	20.557
✓5.50 *	0.6391	6.7115	4.0050	88.0598	20.414
6.00 *	0.5858	6.6894	3.6712	95.8818	20.30%3
6.50 *	0.5408	6.6727	3.3888	103.7175	20.2109
7.00 *	C.5023	6.6572		111.5659	20.1375
7.5C *	0.4687	6.6453		119.4189	20.0771
* 00.8	0.4394			127.2808	20.0268
* 8.50 *	0.4135	6.6269	2.5914	135.1484	19.9845
9.00 *		6.6198	2.4474	143.0208	19.948
* * 9.50 *	0.3700			150.8972	
* * 10.00 *	0.3515	6.6084	2.2027	158.7769	19.891

RYK = 1.00000 POISIONS RATIO = 0.30

NUMBER OF TERMS IN SERIES = 18

<b>中で 4の数を数する たっま</b> かか	(2) 200 年21年21日20日 日本日本日本日本日本日本日本日本日本日本日本日本日本日本日本日本日本日本日	me son son p	E. A 教育 在19 E19 E. 20 E19 E19 E19 E19 E19	Specifics and the mass was not not seen	*
ASPECT *			MODES		*
RATIO *	( () • () )		(1,0)		(1,1) *
1.00 *	3.4937		21.4400	27.4562	31.1718 *
1.50 *	2.3212	7.8173	14.41.84	36.1142	26.4598 *
2.00 #	1.7363	7.4607	0.8050	47.2384	24.3758 *
2.50 *	1.3864	7.2617	8.6350	57.8410	23.1752 *
* 3.00 *	1.1537	7.1403	7.3896	68.6772	22.4324
3.50 *	0.9879	7.0619	6.1582	79.6225	21.9330
4.00 *	0.8638	7.0085	5.3854	90.6509	21.6182
4.5C *	0.7673	6.9706	4.7848	101.7037	21.3725
* 5.00 *	0.6903	6.9429	4.3028	112.7843	21.1903
5.50 *	0.6273	6.9219	3.9123	123.8848	21.0517
# 6.00 #	0.5748	6.9058	3.5854	134.9999	20.9442
6.50	0.5305	6.8931	3.3089	146.1262	20.8337
7.00 *	0.4925	6.8830	3.0720	157.2613	20.7632
7.50	c.4596	5.8747	2.8668	168.4034	20.7056
	* * 0.4308	6.8679	2.6873	179.5569	20.6580
	* 0.4054	6.8623	2.5290	190.7095	20.6182
	* * 0.3829	6.8575	2.3882	201.8660	20.5845
	* * 0.3627	6.8535	2.2624	213.0025	20.5559
• 10.00	* 0.3445	6.8500	2.1491	224.1881	20.5314

RY. = ).CCOCO FCISIENS RATIC = C.8C

NUMBER OF TERMS IN SERIES = 24

CORD ST.	an emile i et vettilendelmetalen en	es el de la son en en labrecia de 2	\$1.751 \$10.00 A	BO NOT BUSED OF BOTH IN BUILD FOR FOR BUILD	A Tentre (elluet) en els sols	1
ASPECT *			MCCES			i ×
RATIC #	(0,0)	(0,1)	(1,0)	(C,2)	(2,1)	\$ **
an e e e e e e e e e e e e e e e e e e e	arri ar l'al l'al ci acci acci acci acci acci acci acci	Bubberanden beberanden.	eme i eule cedero en eure Vi	ilasion pomerci kologo i seco eje seco e co	* Companies and the companies of the com	e: ∰ •
1.00 *	3.4926	8.5275	21.4345	27.2854	31.1496	**
1.50 *	2.3196	7.7892	14.4141	36.0083	26.4243	N N
Z.00 *	2.7345	7.4204	70.7992	46.9760	24.3313	4
2.10 *	1 7 Block	7.2090	8.6281	58.0593	23.1781	- 17 - 18
5.0C #	1.1517	7.0767	7.1819	68.7330	22.4022	77 14
7.50 *	C.9858	6.9886	6.,502	79.6517	21.9446	N
4.00 *	0.8617	6.9189	5.3774	90.6529	21.6091	**
4.5C *	C.7654	6.8727	4.7770	102.7011	21.367	di di
5.0C *	0.6884	6.8383	4.2972	112.7796	21.1873	- TR
5.50 *	0.6255	6.8118	3.9050	23.6792	21.C270	*
6.00 *	0.5731	6.7910	3.5784	134.9943	20.9180	76 76
. C #	C.5289	6.7766	3.3022	146.1209	20.8314	¥
	0.4510	6.7633	3.0656	157.2565	20.7616	74 14 14
7.50 *	C.458	6.750C	2.8607	168.3992	20.7045	**
8.GC *	C.4%94	6.7409	2.6814	179.5476	20.6575	il il
8.50 4		6.7332	2.5234	29C.7CG5	20.6278	
5.00 w		6.7268	2.3829	201.8573	20.5845	9
9.5C *		6.7212	2.2574	213.0173	20.556	ā
ic.cc *	C.3434	6.7165	2.1443	224.775	20.5317	ą ą

RYX= %.CCCCO PCISTONS RATIC= 0.80 NUMBER OF TERMS IN SERIES=80

PUCT *			MCDES		
TIO *	(0,0)	(0,1)	(3,0)	(0,2)	(4,3)
% 00 *	3.4919	8.5268	21.4308	27.3504	
* 5C *	2.3185	7.7880	4.4:34	35.5476	26.2340
	1.7332	7.4181	10.7985	46.8786	24.1940
2.5C *	1.3830	7.2041	8.6273	57.8879	22.9806
* 3.00 *	1.1503	7.0683	7.1809	69.4690	32.2376
* 3.5C *	0.9845	6.9763	6.1490	79.7350	21.73 57
* 4.UC *	0.8604	6.9110	5.3760	90.6840	21.3505
4.5C *	C.7643	6.8628	4.7754	101-7141	23.0840
* 5.00 *	0.6872	6.8264	4.2955	112.7841	20.8834
* 5.50 *	0.6244	6.7981	3.9031	23.8791	20.7286
* * 00.8	0.5720	6.7758	3.5765	134.9914	20.6568
*	0.5278	6.7579	3.3003	146.1164	20.5094
* 7.00 *	C.49CO	6.7432	3.0637	257.2510	20.4203
* 7.50 *	0.4512	6.73%2	2.8588	168.3930	20.7652
* * 00.8	C.4285	6.7211	2. <i>6</i> 795	179.5410	20.311.
* 8.50 *	0.4032	6.7127	2.5215	90.6938	20.2656
* 9.00 *	C.3807	6.7055	2.3810	201.8505	20.2270
9.50 *	0.3606	6.6993	2.2554	213.0106	70.194
10.0C *	C.3426	6.6940			
		TAR	LE NC.= 2	.3.2	

RYX = 0.05000 POISIONS RATIG= 0.20

NUMBER OF TERMS IN SERIES=18

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ASPECT *			MODES		
RATIO *	(0,0)	(0,1)	(1.0)	(0,2)	(1,1)
0.10 *	35.1600	35.4374	220.3457	36 - 2938	220.6619
0.20 *	17.5800	18.1302	110.1728	19.7713	110.8042
0.30 *	11.7200	12.5334	73.4485	14.8458	74.3934
0.40 *	8.7900	9.8528	55.0865	12.7150	56.3422
0.50 *	7.0319	8.3265	44.0693	11.6313	45.6323
0.60 #	5.8599	7.3658	36.7249	11.0359*	<b>经验证证证证</b>
0.70 *	5.0228	6.7186	31.4798	10.7049	33.6253
0.80 *	4.3949	6.2596	27.4056	10.5366	29.9888
0.90 *	3.9065	5.9197	24.4797	10.4794	27.2147
1.00 *	3.5159	5-6592	22.0328	10.5042	25.0432
×2.00 *	1.7578	4.5812	11.0101	12.9688	16.2533
3.00 *	1.1718	4.2313	7.3420	16.9854	13.9809
4.00 *	0.8788	4.0581	5.5064	21-4950	12.9957
5.00 *	0.7030	3.9661	4.4051	26.1984	12.4575
6.00 *	0.5859	5.9141	3.6708	31.0026	12.1247
7.00 *	0.502	3.8783	3.1464	35.8638	11-9041
* * 00.8	0.4393	3.8513	2.7530	40.7606	11.7506
9•00 <b>*</b>	0.3905	J.8343	2.4473	45.6811	11.6398
* 10.00	0.3515	3.8219	2.2024	50.6180	11.5574

EYA = 0.06075 POISIONS RATIC= 0.14 NUMBER OF TERMS IN SERIES = 18

SPOCT *			MODES			<b>.</b> ≰
OITA	(0,0)	(0,2)	(3,0)	(0,2)	( ** , ) )	
n anders en en 🐠		kan kuu maa dan probesia oo kade k	n de la compania del compania del compania de la compania del la compania de la c	<ul> <li>*** ** *** *** *** *** *** *** *** ***</li></ul>		**
0.0 4		35.4781	210.3457	36.4.589		
0.20 ¥	17.5800	28.2102	1.0.1728	20.0823	10.9033	
0.0	3. <b>. 7</b> . 99	2.5505	73.4485	15.2737	74.5415	
0.40 *	8.7899	_J.0030	55.0865	13.23.9		
3.50 *	7.0218	8.5048	44.0698	12.217	45.8E04	
0.60 *	5.8598	7.5640	36.7264	11.6808	38.375	
0.70 *	5.0226	6.9374	28.7047	11.4066	33.956.	
9.80 *	5.3947	6.49.4	27.5332	11.2970		
0.90 *	3.9064	6.1614	24.4786	11.3022	27.628	
00 *	3.5157	5.9074	22.0319	11.2935	25.5040	
2.00 *	1.7575	4.8392	11-0066	14.0633	16.9190 ·	
7.00 W	.1715	4.4895	7.3393	19.5210	14.7120	
		244	5.5042	24.9276	13.7515	
5.00 +	ŭ.7,028	4.2555	4.4031	30.4962	13.2252	
6.00 *			3.6691	36. 684	1.2.8976	
7.06 *	0.5019	6. 56.67	3.1449	44.8951	12.6828	
8.00 *		4.12.2	2.77.17	47.6569	12.5342	
9.00 *	0.390~	4.1034	2.4459	53.420	12.4273	
* 00.00	0.3513	4.0916	2.2015	59.7435	12.3481	
entropos e e e e	k 1 - Angel Barragan Fran Base Book alam entraka	AL Magazan pagaran a	ing the state of t	ാവുള്ള വരുന്നു.	BURNES BARROTAN STREET	
		TAB	LE NO.= 2.	. 0		

RYX = 0.50000 POISIONS RATIO= 0.05 NUMBER OF TERMS IN SERIES=18

ASPECT :			MCDES		
RATIO +	6 (0,0) 6 5 a. no arr eo ero ameno eso esa	(O, )	( ) + O )	(0,2) • ====================================	1 + 1 )
0.30	35-1600	36.0417	220.3457	38-6922	221.3511
0.20		19.2944	110.1729	24.0097	112.1745
0.30	11.7199	14-1741	73.4483	20.3137	76.4315
0.40	8.7899	11.8663	55.0888	19.0429	58.9990
0.50		10.6112	44.0653	18.6885	48.9050
0.60	5.8598	9.8375	36.7228	18.8211	42.4422
0.70	5.0227	9.3130	31.4774	19.2683	37.4622
0.80	4.3948	8.9319	27.5438	19.9388	34.7916
0.90	3.9060	8-6398	***	20.7742	32.4521
1.00	3.5158	8-4067	21.8164	21.6875	30.6624
#2.00 *	1.7578	7-3548	11-0146	34.6349	23.8149
5.00		7.0535	7.3429	49.4485	22.0067
4.00 *	0.8788	6.9175	5.5029	64.7697	21.2196
5.00	0.7030	6.8533	4.4056	80.2912	20.8071
6.00	0.5859	6.8170	3.6713	95.9126	20.5659
7.00		6.7945	3.1468	111.5910	20.4135
8.00	* 0.4394	6.7797	2.7534	27.3049	20.3965
9.00		6.7694	2.4475	143.0424	20.3322
10.00	• 0.3515 •		2.2027		20.2858

RYK = 1.00000 POISIONS RATIO= 0.30 NUMBER OF TERMS IN SERIES=18

* ASPECT *			MCDES		ক্ষা হ'ল। আন্ত প্ৰথম একে স্থাপ প্ৰচান আৰু চন্দ্ৰ চন্দ্ৰ চন্দ্ৰ বুঁ
RATIO *	(0,0)				(1,1)
**************************************					221.4828
0.20 *	17.5742	19.2930	110.1721	24 • 3 4 5 8	112.4926
0.30 *	11.7104	14.2261	73.5104	21.0952	· 法保持条件条件。
0.40 *	8.7771	11.9669	54.1262	20.3201	59.3435
0.50 *	7.0164	10.7433	43.9152	20.5153	49.6916
0.60 *	5.8423	9.9842	36.6652	21.2297	40.9240
0.70 *	5.0031	9-4639	31.5357	22.2405	38.0155
0.80 *	4.3741	9.0805	27.9258	23.2774	35.1180
0.90 *	3.8849	8.7831	23.2218	26.4118	32.892
1.00 *	3.4937	8.5441	21.4400	27.4561	31.1718
<b>≠2.</b> 00 *	1.7363	7-4607	10.8050	47.2348	24.3758
3.00 *	1.1537	7.1403	7.1896	68.6772	22.4324
4.00 *	0.8638	7.0035	5.3854	90.6509	21.6183
5.00 *		6.9429	4.3048	112.7843	21.1906
6.00 *		6.9058	3.5854	34.9999	20.9442
7.00 *	0.4925	6.8830	3.0720	157.2613	
* 00.8	0.4308	6.8679	2.6879	± <b>7</b> 9 <b>•</b> 5569	20.6580
9.00 #	0.3829	6.8575	2.3882	201.8660	20.5845
10.00 * *	0.3445			224. 881	
www.wi/2 研究 展示性 (2012年代) 2 新刊 (2013年代)	No. of Section And Section 1998		LE NO.= 2		

RYX = 0.06875 MODE (0,0)

EFFECT OF POISIONS RATIO ON FREQUENCY PARAMETER.

and the supplemental supplements	A. · · · · · · · · · · · · · · · · · · ·		140 140 150 CIN \$50 CIN 150 150 150 150 150 150 150 150 150 150		· · · · · · · · · · · · · · · · · · ·
ASPECT *		POIS	IONS RATIO	0	4
RATIO *	0.025	0.05	0.10	0.20	0.30 +
ena en ana en a en a en a en a en a en	2 查許 2023年2月 東京公司職 有 3 包25 約3 集成6 日		- 100 etc 600 t pa 600 etc 500 b pa 1		ായതായത്തെയുടെ അവ
1.00 *	3.5160	3.5160	3.5159	3.5158	3.5),55
1.50 *	2.3440	2.3440	2.3439	2.3437	2.3433
2.00 *	2.7580	7580	1.7579	1.7577	1.7573
2.50 *	1.4064	1.4064	1.4063	4.4061	1.4057
3.00 *	1.1720	1.1720	1.1719	1.1717	1.1713
3.50 <b>*</b>	1.0046	1.0046	1.0045	1.0043	1.0039
4.00 *	0.8790	0.8790	0.8789	0.8787	0.8783
4.50 *	0.7813	0.7813	0.7813	0.7810	0.7807
5.00 *	0.7032	0.7032	0.7031	0.7029	0.7026
5.50 <b>*</b>	0.6393	0.6393	0.6392	0.6390	0.6387
6.00 *	0.5860	0.5860	0.5859	0.5857	0.5854
6.50 <b>*</b>	0.5409	0.5409	0.5409	0.5407	0.5404
7.00 *	0.5023	0.5023	0.5022	0.5020	0.5017
7.50 *	0.4688	0.4638	0.4687	0.4686	0.4683
8.00 *	0.4395	0.4395	0.4094	0.4393	0.4390
8.50 *	0.4135	0.4136	0.4136	0.4134	0.4132
9.00 *	0.3907	0.3907	0.3906	0.3905	0.3902
9.50 *	0.3701	0.3701	0.3701	0.3699	0.3697
* 10.00 *	0.3516	0.351.6	0.3516	0.3514	0.3512
*	n 120 mm kg gra 180 kan 800 pro 120 i				

RYX = 0.06875 MODE (0,1)

EFFECT OF POISIONS RATIO ON FREQUENCY PARAMETER.

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ASPECT #		POIS	IONS RATI	0		<b>*</b>
RATIO *		0.05	0.10	0-20	0.30	* *
ស្រួល ស លោខភាពនេះ បនា។ <b>-</b> គ្គ	Sign of the state		no del con del del del del con del del		_ 10 E3 () 60 E	*
1.00		5.9904	5.9676	5.9262	5.8789	*
1.50	5.2852	5.2736	5.2502	5.2085	5.1545	*
2.00	4.9366	4.9248	4.9010	4.8590	4.8037	*************************************
2.50		4.7235	4.6989	4.6490	4.5980	长
3.00	, - 10 - 100 mm	4.5789	4.5541	4.5100	4.4531	*
3.50		4.4846	4.4594	4.4139	4.3566	Ti Fi
4.00 *	4.4299	4.4171	4.3916	4.3398	4.2873	*
4.50 #	4.3852	4.3723	4.3463	4.2892	4.2361	景丛
5.00	4.3472	4.3348	4.3079	4.2549	4.1973	*
5.50 *	4.3178	4.3046	4.2782	4.2253	4.1707	。 **
6-00 *	4.2913	4.2782	4.2548	4.2011	4.1466	*
6.5C *	The same of the same	4.2599	4.2333	4.1820	4.1248	*
7.00 **	4.2585	4.2452	4.2184	4.1666	4.1116	长
7.50 *	4.2464	4.2330	4.2061	4.1518	4.0991	*
9.00 *		4.2229	4.1960	4.1415	4.0883	*
8.50 #		4.2145	4.1889	4.1328	4.0789	*
9.00 #	4.2208	4.2073	4.1815	4.1270	4.0713	长龄
9.50 *	4.2147	4.2012	4.1740	4.1192	4.0647	
10.00	4.2094	4.1959	4.1687	4.1138	4.0591	
	n de la gree and			は		<b>3</b> 201

RYX = 0.07 MOCE(1,0) EFFECT OF PCISIONS RATIO ON FREQUENCY PARAMETER.

1.00 * * * * * * * * * * * * * * * * * *	22.0345 12.8075 11.0172	6.2954 5.5085	22.0341 12.7718 11.0155 8.8127 7.3439 6.2947	12.6895* 11.0099 8.8091 7.3410 6.2922	22.0303 ******* 11.0005 8.8032 7.336; 6.2879
1.00 * * 1.50 * * 2.00 * * 2.50 * * 3.50 * * 4.00 * 4.50 * 5.00 *	12.8075 11.0172 8.8138 7.3448 6.2955 5.5086	12.7832 11.0168 8.8135 7.3446 6.2954 5.5085	12.7718 11.0155 8.8127 7.3439 6.2947	12.6895* 11.0099 8.8091 7.3410 6.2922	******* 11.0005 8.8032 7.336; 6.2879
1.50 * 2.00 * 2.50 * 3.00 * 3.50 * 4.00 * 4.50 * 5.00 *	11.0172 8.8138 7.3448 6.2955 5.5086	11.0168 8.8135 7.3446 6.2954 5.5085	11.0155 8.8127 7.3439 6.2947	11.0099 8.8091 7.3410 6.2922	11.0005 8.8032 7.336; 6.2879
2.0C * 2.5C * 3.0C * 3.5C * 4.0C * 4.5C * 5.0C *	8.8138 7.3448 6.2955 5.5086	8.8135 7.3446 6.2954 5.5085	8.8127 7.3439 6.2947	8.8091 7.3410 6.2922	8.8032 7.336; 6.2879
2.50 * * 3.50 * * 4.00 * * 4.50 * * 5.00 *	7.3448 6.2955 5.5086	7.3446 6.2954 5.5085	7.3439 6.2947	7.3410 6.2922	7.336; 6.2879
3.00 * 3.50 * 4.00 * 4.50 * 5.00 *	6.2955 5.5086	6.2954 5.5085	6-2947	6.2922	6.2879
3.50 * 4.00 * 4.50 * 5.00 *	5.5086	5.5085			
4.00 * 4.50 * 5.00 *			5.5079	S FORE	
* 5.00 *	4.8965	4 0044		0.000	5.5017
		4.8964	4.8959	4.8937	4.8902
	4.4069	4.4068	4.4063	4.4043	4.4010
5.50 *	4.0062	4.0061	4.0057	4.0039	4.0008
6.00 * *	3.6724	3.6723	3.6719	3.6701	3.6673
6.5C *	3.3899	3.3898	3.3894	3.3878	3.3851
7.0C *		3.1477		3.1458	
7.5C *		2.9373		2.9360	
8.00 *		2.7542			
*					
*					
9.50 *		2.3193			
	2.2034	2.2034	2.2031	2.2019	2.2001
	TABLE NO.=	= 3.20			

PYX = 0.06875 MODE (1.1)

EFFECT OF POISIONS RATIO ON FREQUENCY PARAMETER.

1		end to the size has the size the the size and the size the size the size that the size the size the size that the size the size that the size	7 and 1856 the 1856 the 1856 the 700 1876 the 1876 the 18			k Kirila Arada Arada Arada (Arada Arada (Arada Arada) (Arada Arada) (Arada Arada) (Arada Arada) (Arada Arada)	**
1	, , , , , , , , , , , , , , , , , , ,	* 0 025		SIONS RATI		0.70	*
1	RATIO	* 0.025 *	0.05	0.10	0.20	0.30	*
I	1.60	* * 25.6270		25.5785			*
1		* * 19.6998	19.6771	19.6309		19.4361	發發
ľ	2.00	* * 17.1463	17.1206	17.0687	16.9624	16.8528	<b>张</b> ¥
ľ	2.50	* * 15.7972	15.7692	15.7126	15.5973	15.4788	<b>禁</b>
Ĺ	3.00	* 14.9807	14.9509	14.8909	14.7685	14.6365	*
ļ	3.50	* 14.4251	14.3940	14.3313	14.2037	14.0731	并發
a ¥	4.00	* 14.0348	14.0025	13.9375	13.8052	13.6701	*
# #	4.50	* 13.7446 *	13.7114	13.6443	13.5081	13.3692	상 삼
ë ë	5.00	* 13.5223 *	13.4881	13.4193	13.2798	13.1439	養養
#	5.50	* 13.3478	13.3129	13.2426	13-1001	12.9550	*
ا امر ا	6.00	* 13.2085 *	13.1729	13.1014	12.9563	12.8087	*
i i	6.50	* 13.0954 *	13.0593	12.9866	12.8359	12.6896	安
} }	2 W 45 G	* 13.0025 *	12.9660	12.8923	12.7432	12.5915	茶
<b>t</b> b		* 12.9253	12.8883	12.8183	12.6631	12.5098	*
H N		* 12.8605 *	12.8231	2.7479		12.441	分
¥		*			1.2.5386		*
#		*			12.4898		*
*					12.4477		装
*	10.00	* 12.6834 *					*

POI SIONS RATIO= 0.25 MODE(0,0)

EFFECT OF RYX ON FREQUENCY PARAMETER.

SPECT *			RYX		*
ATIO *	0.05	0.25	0.50	0.75	1.00
1.00 *	3.5158	3.5138	3.5102	3.5058	3.5009
1.50 *	2.3437	2.3415	2.3377	2.3334	2.3286
* 2.00 *,	1.7577	1.7554	1.7518	1.7477	1.7433
2.50 *	1.4061	1.4093	1.4005	1.3968	1.3928
* 3.00 *	1-1717	1.1696	1.1665	1.1631	1.1595
3.50 *	1.0042	1.0023	0.9994	0.9964	0.9932
<b>4.00 *</b>	0.8787	0.8768	0.8742	0.8715	0.8686
* 4.50 *	0.7810	0.7793	0.7769	0.7744	0.7718
5.00 <b>*</b>	0.7029	0.7013	0.6991	0.6967	0.6944
* 5.50 *	0.6390	0-6375	0.6354	0.6333	0.6311
* 6.00 *	0.5857	0.5843	0.5824	0.5804	0.5784
6.50 #	0.5407	0.5393	,0.5375	0.5357	0.5338
7.00 *	0.5020	0.5008	0.4991	0.4974	0.4956
* 7.50 *	0.4685	0.4674	0.4658	0.4642	0.4625
* 8.00 *	0.4393	0.4381	0.4366	0.4351	0.4335
* 8.50 *	0.4134	0.4123	0.4109	0.4095	0.4080
9.00 *	0.3904	0.3894	0.3881	0.3867	0.3853
9.50 *	0.3699	0.3689	0.3676	0.3663	0.3650
10.00 *	0.3514	0.3505	0.3492	0.3480	0.346

POISIONS RATIO= 0.25 MODE(0,1)

EFFECT OF RYX ON FREQUENCY PARAMETER.

PECT *			RYX		4
* 01T	0.05	0.25	0.50	0.75	1.00 *
1.00 *	5.6409	7.1700	7.9534	8.4276	8.7582
1.50 *	4.9061	6.4601	7.2479	7.7159	8.0362
* 2.00 *	4.5616	6.1120	6.8874	7.3569	7.6842
2.50 *	4.3511	5.8979	6.6850	7.1583	7.4886
* 3.00 *	4.2118	5.7668	6.5600	7.0372	7.3702
* 3.50 *	4.1136	5.6843	6.4781	6.9586	7.2938
4.00 *	4.0427	5.6227	6.4219	6.9049	7.2418
* 4.50 *	3.9898	5.5745	6.3818	6.8668	7.2050
* 5.00 *	3.9494	5.5455	6.3522	6.8388	7.1781
5.50 *	3.9184	5.5197	6.3299	6.8177	7.1578
6.00 *	3.8929	5.4979	6.3143	6.8015	7.1422
6.50 *		5.4826	6.3003	6.7887	7.1299
7.00 *		5.4704	6.2890	6.7784	7.1201
7.50		5.4603	6.2799	6.7701	7.1121
8.00		5.4521	6.2724	6.7632	7.1055
•	* * 3.8206	5.4452	6.2661	6.7575	7.1001
	* * 3.8127	5.4393	6.2608	6.7527	7.0959
	* 3.8075	5.4344	6.2562	6.7486	7.0916
10.00	* * 3.8002	5.4301	6.2524	6.7451	7.088

PCISIONS RATIO= 0.25 MODE(1,0)

EFFECT OF RYX ON FREQUENCY PARAMETER.

*			0.77		
SPECT *		0.05	RYX 0.50	0.75	1.00
RATIO *	0.05	0.25	0.30		
* 1.00 *	22.0318	22.0473	21.7218	21.6005	21.6327
1.5C *	14.6917	14.6355	14.5965	14.5516	14.5042
2.00 *	11.0057	10.9837	10.9483	10.9108	10.8718
2.5C *	8.8083	8.7863	8.7560	8.7241	8.6912
* 3.00 *	7.3405	7.3210	7.2943	7.2668	7.2383
* 3.50 *	6.2918	6.2743	6.2508	6.2263	6.2012
* 4.00 *	5.5052	5.4894	5.4683	5.4463	5.4239
<b>4.50</b> *	4.8934	4.8790	4.8598	4.8400	4.8197
* 5•00 *	4.4040	4.3907	4.3732	4.3551	4.3367
5.50 *	4.0036	3.9913	3.9751	3.9585	3.9416
* 6.00 *	3.6699	3.6585	3.6435	6.6281	3.6125
<b>6.50</b> *	3.3875	3.3769	3.3629	3.3486	3.3342
7.00 *	3.1455	3.1355	3.1225	3.1091	3.0956
7.50 *	2.9358	2.9254	2.914)	2.9016	2.8890
* * 00 *	2.7523	2.7434	2.7318	2.7201	2.7082
* 8.50 *	2.5904	2.5819	2.5710	2.5599	2.5487
* 9.00 *	2.4464	2.4384	2.4281	2.4176	2.4069
* 9.50 *	2.3177	2.3100	2.3002	2.2902	2.2801
* 10.00 * *	2.2018	2.1945	2.1851	2.1756	2.1660

POISIONS RATIO= 0.25 MODE(1,1)

EFFECT OF RYX ON FREQUENCY PARAMETER.

SPECT *			RYX		
* * OITA *	0.05	0.25	0.50	0.75	1.00
1.00	25.0205	27.9045	29.7041	30.8570	39.6121
1.50	18.8785	22.6490	24.7732	26.0949	27.0325
2.00	16.2122	20.3981	22.6467	24.0190	24.9574
2.50	14.7928	19-1838	21.4526	22.8338	23.7998
3.00	* • 13.9292	18.4092	20.7101	22.1012	23.0730
3.50	13.3627	17-8854	20.2261	21.6386	22.5859
4.00	* * 12.9442	17.5152	19.8529	21.2951	22.2847
4-50	* 12.6386	17.2415	19.5925	21.0515	22.0310
5.00	* * 12-4031	17-0600	19.3963	20.8707	21.8523
5.50	* * 12.2174	16-8981	19.2453	20.7332	21.7155
6.00	* * 12.0681	16.7820	19-1266	20-6264	21.6339
6.50	* * 11.9463	16.6857	19.0319	20.5420	21.5521
7.00	* * 11.8458	16.6072	18.9552	20.4741	21.4866
7.50	* * 11.7618	16.5429	18.8922	20.4189	21.4332
8.00	* 11.6910	16.4896	18.9160	20.3732	21.3892
8.50	* 11.6308	16.4450	18.8758	20.3352	21.3525
9.00	* * 11.5792	16.4073	18.8419	20.3031	21.3216
9.50	* * 11.5347	16.3752	18.8130	20.2759	21.2953
10.00	# # 11.4960	16.3477	18.7883	20.2525	21.2728

RYX = 0.06875 POISIONS RATIO = 0.24 NUMBER OF TERMS IN SERIES=18 FREQUENCY PARAMETER FOR FREE PLATE

PECT *			MCDES		*
* TIC *	(C,O)	(0,1)	(1,0)	(1,1)	(2,2)
* 0.10 *	-0.0000	-0.0000	-0.0000	7.6518	0.5857
* 0.20 *	-0.0000	-0.0000	-0.0000	7.6604	1.1717
* 0.50 *	-0.0000	-0.0000	-0.0000	7.6738	1.7572
* 0.40 *	-0.0000	-0.0000	-0.0000	7.6910	2.3430
* 0.50 *	-c.0000	-0.0000	-0.0000	7.7109	2.9288
* 0.60 *	-0.0000	-0.0000	-0.0000	7.7322	3.5148
* C.70 *	-0.0000	-0.0000	-0.0000	7.7538	4.1007
0.80 *	-0.0000	-0.0000	-0.0000	7.7750	4.6856
0.9C *	-0.0000	-0.0000	-0.0000	7.795%	5.2724
* 1.00 *		-0.0000	-0.0000	7.8134	5.8583
* .70 *		-0.0000	-a.caao	7.6873	11.8232
\$ (a) *	-0.0000	-0.0000	-0.0000	7.8527	7.598
* 4.00 *		-0.0000	-0.000	7.9051	23.4555
5.00 t	-0.0000	-0.0000	-0.0000	7.7673	29.343
6.00 ×		-0.0000	-O.CCCO	7.7399	
	* -0.0000	-0.0000	-0.0000	7.7203	42.0658
8.00	* * -0.0000	-0.0000		7.706	
N. San	* * -0.0000	-0.0000	-0.6000	7.6955	
10.00	* * -0.0000 *	-0.0000	-0.0000	7.6876	58.6636

DESIGN TABLES FOR MODE (0.0) OF CANTILEVER PLATE OF ASPECT RATIC= 1.0

* RYX *		POISIONS RATIO					
* *	0.025	0.05	0.10	0.20	0.30		
0.05 *	3.5160	3.5160	3.5160	3.5159	3.5159		
0.25 *	3.5160	3.5159	3.5157	3.5146	3.5127		
0.50 *	3.5159	3.5158	3.5151	3.5125	3.5074		
* 0.75 *	3.5159	3.5156	3.5145	3.5096	3.5010		
* 1.00 *	3.5159	3.5154	3.5138	3.5066	3.4937		

# DESIGN TABLES FOR MODE(0,0) OF CANTILEVER PLATE OF ASPECT RATIO= 2.0

* RYX *		POISI	ONS RATIO		
*	0.025	0.05	0.10	0.20	0.30
0.05 *	1.7580	1.7580	1.7579	1.7578	1.7575
* 0.25 *	1.7580	1.7579	1.7576	1.7564	1.7542
* 0.50 *	1.7579	1.7578	1.7571	1.7541	1.7490
* 0.75 *	1.7579	1.7576	1.7564	1.7516	1.7429
* 1.00 *	1.7579	1.7575	1.7558	1.7488	1.736

DESIGN TABLES FOR MODE(0,0) OF CANTILEVER PLATE OF ASPECT RATIC= 3.0

RYX *		POIS	POISICNS RATIO		
* * 	0.025	0.05	0.10	0.20	0.30
0.05 *	1.1720	1.1720	1.1719	1.1718	1.1715
0.25 *	1.1720	1.1719	1.1716	1.1705	1.1689
0.50 *	1.1719	1.1718	1.1711	1-1685	1.1639
0.75 *	1.1719	1.1717	1.1706	1.1664	1.1589
1.00 *	1.1719	1.1715	1.1701	1.1642	1.1536

# DESIGN TABLES FOR MODE(0.0) OF CANTILEVER PLATE OF ASPECT RATIO= 4.0

1 77		POISI	POISIONS RATIO		
•	* * 0.025 *	0.05	0.10	0.20	0.30
0.05	* * 0.8790	0.8790	0.8789	0.8788	0.8785
0.25	* 0.8790	0.8789	0.8787	0.8776	0.8759
0.5C	* 0.8790	0.8788	0.8783	0.8760	0.8721
0.75	* .0.8789	0.8787	0.8778	0.8742	0.8679
1.00	* <b>0.878</b> 9	0.8786	0.8774	0.8724	0.8636

### DESIGN TABLES FOR MODE (0.0) OF CANTILEVER PLATE OF ASPECT RATIC= 5.0

*					
RYX * * * *	0.025	POISI 0.05	O.10	0.20	0.30
* 0.05 *	0.7032	0.7032	0.7032	0.7030	0.7028
* 0.25 *	0.7032	0.7031	0.7029	0.7020	0.7004
* 0.5C *	0.7032	0.7030	0.7026	0.7006	0.6972
* 0.75 *	0.7031	0.7030	0.7022	0.6991	0.6937
1.00 * *		0.7029	0.7018	0.6976	0.6902

## DESIGN TABLES FOR MODE (0,0) OF CANTILEVER PLATE OF ASPECT RATIC= 6.0

* RYX *	(2) 20 (1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1	POISI	CNS RATIO		
*	0.025	0.05	0.10	0.20	0.30
* * 0.05 *	0.5860	0.5860	0.5860	0.5858	0.5856
*		0.5859	0.5850	0.5849	0.5835
. *		0.5859	0.5854	0.5837	0.5807
0.50 * *		0.5858	0.5851	0.5824	0.5778
0.75 * 1.00 *		0.5857	0.5848	0.5812	0.5748

DESIGN TABLES FOR MODE(0,0) OF CANTILEVER PLATE
OF ASPECT RATIC= 7.0

* RYX *		POISIONS RATIO					
* *	0.025	0.05	0.10	0.20	0.30 * * *		
·* * 0.05 *	0.5023	0.5023	0.5022	0.5021	0.5C19 *		
* 0.25 *	0.5023	0.5022	0.5020	0.5013	0.5CO1 *		
0.50 *	0.5023	0.5022	0.5018	0.5003	0.4976		
0.75 *	0.5022	0.5021	0.5015	0.4992	0.4951		
1.00 *	0.5022	0.5020	0.5012	0.4980	0.4924		

# DESIGN. TABLES FOR MODE(0.0) OF CANTILEVER PLATE OF ASPECT RATIC= 8.0

* * XY		POISI	ONS RATIO	<b>,</b> .	
*	0.025	0.405	0.10	0.20	0.30
<del>*</del>	0.4395	0.4395	0.4395	0.4393	0.4392
0.05 * *	0.4395	0.4394	0.4393	0.4386	0.4375
* 0.50 *	0.4395	0.4394	0.4390	0.4377	0.4353
* 0.75 *		0.4393	0.4388	0.4367	0.4331
* 1.00 *		0.4393	0.4386	0.4357	0.430

### DESIGN TABLES FOR MODE (0,1) OF CANTILEVER PLATE OF ASPECT RATIC= 1.0

RYX	*	POISIONS RATIO					
	* * 0.025 *	0.05	0.10	0.20	0.30		
0.05	* * * 5.717	5 5.7085	5.6955	5.6592	5.6226		
0.25	* * 7.450	5 7.4198	7.3655	7.2363	7.0980		
0.50	* * 8.448	5 8.4067	8.2897	8.0685	7.8352		
0.75	* * 9.113	6 9.0541	8.8956	8.5888	8.2609		
1.00	* 9.625	9.5477	9.3517	8.9637	8.5441		

### DESIGN TABLES FOR MODE(0.1) OF CANTILEVER PLATE OF ASPECT RATIO= 2.0

YX *		POISI	ONS RATIO		and the
* *	0.025	0.05	0.10	0.20	0.30
0.05 *		4.6313	4.6127	4.5812	4.5368
*	6.4152	6.3825	6.3164	6.1812	6.0416
1	* * 7.4105	7.3548	7.2508	7.0154	6.7636
	* * 8.0833	8.0067	7.8506	7.5261	7.1824
	* * 8.6029	8.5068	8.3107	7.9000	7.460

### DESIGN TABLES FOR MODE(0,1) OF CANTILEVER PLATE OF ASPECT RATIC= 3.0

* RYX *		POISI	ONS RATIO		
* * *	0.025	0.05	0.10	0.20	0.30
*- * 0.05 *	4.3000	4.2903	4.2707	4.2313	4.1913
* 0.25 *	6.0797	6.0459	5.9776	5.8381	5.6997
* 0.50 *	7.1108	7.0535	6.9279	6.6910	6.4320
* 0.75 *	7.7965	7.7167	7.5544	7.2121	6.8574
* 1.00 * *	8.3259	8.2272	8.0226	7.5925	7.1403

## DESIGN TABLES FOR MODE(0,1) OF CANTILEVER PLATE OF ASPECT RATIO= 4.0

RYX *	POISIONS RATIO						
* *	0.025	0.05	0.10	0.20	0.30		
* * 0.05 *	4.1282	4.1183	4.0983	4.0581	4-0221		
* * 0.25 *	5.9443	5.9095	5.8393	5.6915	5.5443		
* 0.50 *	6.9768	6.9175	6.8014	6.5496	6.2914		
* 0.75 *	7.6710	7.5899	7.4249	7.0827	6.722		
* 1.00 *	8.2063	8.1051	7.8986	7.4675	7.008		

### DESIGN TABLES FOR MODE(0.1) OF CANTILEVER PLATE OF ASPECT RATIC= 5.0

	POISIONS RATIO						
0.025	0.05	0.10	0.20	0.30			
	4.0327	4.0116	3.9661	3.9284			
	5.8323	5.7644	5.6160	5.4668			
	6.8533	6.7344	6.4839	6.2203			
*	7.5303	7.3660	7.0206	6.6543			
	8.0487	7.8424	7.4057	6.9429			
	4.0430 4.0430 5.8675 4.6.9133 4.7.6145	POISI  0.025 0.05  4.0430 4.0327  5.8675 5.8323  6.9133 6.8533  7.6145 7.5303	POISIONS RATIO  0.025 0.05 0.10  4.0430 4.0327 4.0116  5.8675 5.8323 5.7644  6.9133 6.8533 6.7344  7.6145 7.5303 7.3660	POISIONS RATIO  0.025 0.05 0.10 0.20  4.0430 4.0327 4.0116 3.9661  5.8675 5.8323 5.7644 5.6160  6.9133 6.8533 6.7344 6.4839  7.6145 7.5303 7.3660 7.0206			

### DESIGN TABLES FOR MODE(0.1) OF CANTILEVER PLATE OF ASPECT RATIO= 6.0

* * XY	POISIONS RATIO						
* *	0.025	0.05	0.10	0.20	0-30		
0.05 *	3.9872	3.9768	3.9560	3.9141	3.8717		
* 0.25 *	5.8263	5.9708	5.7190	5.5726	5.4246		
* 0.50 *	6.8790	6.8170	6.6946	6.4425	6.179		
* 0.75 *	7.5791	7.4968	7.3306	6.9834	6.615		
* 1.00 *	8.1206	8.0170	7.8081	7.3709	6.905		

DESIGN TABLES FOR MODE (0,1) OF CANTILEVER PLATE OF ASPECT RATIO= 9.0

RYX *		POISI	ONS RATIO			
*		0.05	0.10	0.20	0.30	
	* * * 3.9090	3.8984	3.8772	3.8343	3.7924	
	* * 5.7723	5.7358	5.6632	5.5155	5.3626	
	* * 6.8304	6.7694	6.6459	6.3916	6.1266	
	* * 7.5361	7.4532	7.2844	6.9345	6.5657	
1.00	* * 8.0793	7.9750	7.7651	7.3255	6.8757	

## DESIGN TABLES FOR MODE(0.1) OF CANTILEVER PLATE OF ASPECT RATIO= 10.0

		POISIONS RATIO		0.30
0.025	0.05	0.10		
3.8968	3.8852	3.8660	3.8219	3.7724
	5.7272	5.6544	5.5062	5.3532
	6.7620	6.6383	6.3836	6-1182
	7.4454	7.2775	6.9271	6.5579
8.0730	7.9697	7.7583	7.3183	6.8500
	3.8968 5.7632 6.8230 7.5294	3.8968 3.8852 5.7632 5.7272 6.8230 6.7620 7.5294 7.4454	3.8968 3.8852 3.8660 5.7632 5.7272 5.6544 6.8230 6.7620 6.6383 7.5294 7.4454 7.2775	3.8968 3.8862 3.8660 3.8219 5.7632 5.7272 5.6544 5.5062 6.8230 6.7620 6.6383 6.3836 7.5294 7.4464 7.2775 6.9271

DESIGN TABLES FOR MODE(1,1) OF FREE PLATE OF ASPECT RATIO: 1.0

RYX	*	PDISIONS RATID						
	*	0.025	0.05	0.10	0.20	0.30		
, Anna radio senso, pilipo senso-	~~- *			Million villatin salahin makin million majaga upatan kalaga yangan.				
0.05	*	7.4741	7.4539	7.4133	7.3313	7.2483		
0.25	*	11.3354	11.2558	11.1282	10.8452	10.5539		
0.50	*	13.5566	13.4398	13.2026	12.7136	12.2027		
0.75	*	15.0440	14.8841	14.5585	13.8816	13.1656		
1.00	*	16-1911	15.9913	15.5829	14.7280	13.8137		

DESIGN TABLES FOR MODE(1,1) OF FREE PLATE OF ASPECT RATIO= 2.0

<b>*</b>	R <b>YX</b>	* *		POISIONS RATID					
*		*	n de la companya de La companya de la co						
*		* *	0.025	0.05	0.10	0.20	0.30		
* *		-*- *							
* *	0.05	*	7.7096	7.6889	7.6473	7.5632	7.4781		
* *	0.25	* *	11.6746	11.6029	11.4580	11.1620	10.8570		
* *	0.50	* *	13.9197	13.7972	23.5485	13.0357	12.5000		
	0.75	*	15.4129	15.2453	14.9040	14.1948	13.4453		
*	1.00	*	16.5605	15.3511	15.9236	15.0293	14.0745		

DESIGN TABLES FOR MODE(1,1) OF FREE PLATE OF ASPECT RATIO= 3.0

RYX	*		POTS	IONS RATI	:n	
	*					
	* *	0.025	0.05	0.10	0.20	0.30
	*				AND THE PERSON NAMED AND PARTY OF THE PERSON NAMED AND PARTY.	
0.05	*	7.8345	7.8131	7.7703	7.6838	7.5962
0.25	*	11.7972	11.7237	11.5752	11.2720	10.9598
0.50	*	14.0335	13.9034	13.6547	13.1318	12.5861
0.75	*	15.5203	15.3496	15.0023	14.2811	13.5199
1.00	*	16.6629	16.4502	16.0158	15.1082	14.1403

### DESIGN TABLES FOR MODE(1,1) OF FREE PLATE OF ASPECT RATIO= 4.0

RYX	*	PDISIONS RATIO					
	* *	0.025	0.05	0.10	0.20	0.30	
0.05	*- * 5 *	7.8973	7.8755	7.8319	7.7438	7.6546	
0.2	* 5 *	11.8491	11.7747	11.6245	11.3179	11.0024	
0.50	* ) * *	14.0793	13.9531	13.6972	13.1699	12.6200	
0.7		15.5625	15.3906	15.0407	14.3145	13.5485	
1.00	* (*	16.7027	15.4835	16.0513	15.1382	14.1651	

DESIGN TABLES FOR MODE(1.1) OF FREE PLATE OF ASPECT RATIO= 5.0

RYX	* *		POIS	IONS RATI	:o	
	* * -*-	0.025	0.05	0.10	0.20	0.30
	*					
0.05	*	7.9314	7.9054	7.8653	7.7763	7.6861
0.25	*	11.8751	11.8003	11.6492	11.3408	11.0235
0.50	* *	14.1018	13.9750	13.7183	13.1885	12.6364
0.75	*	15.5830	15.4140	15.0592	14.3306	13.5622
1.00		16.7218	15.5059	16.0683	15.1526	14.1770

DESIGN TABLES FOR MODE(1,1) OF FREE PLATE OF ASPECT RATIO= 6.0

		*								
RY	X	* *	POISIONS RATIO							
		* * *	0.025	0.05	0.10	0.20	0.30			
0	•05	* * *	7.9516	7.9295	<b>7.</b> 8850	7.7954	7.7047			
0	- 25	*	11.8898	11.8147	11.8147	11.3537	11.0354			
0	.50	*	14.1143	13.9872	13.7295	13.1988	12.6455			
0	.75	*	15.5944	15.4215	15.0695	14.3395	13.5697			
1	•00	*	16.7324	15.5171	16-0778	15.1603	14.1835			

DESIGN TABLES FOR MODE(1.1) OF FREE PLATE OF ASPECT RATIO= 7.0

RYX	*		POIS	ONS RATIO		
	* *	0.025	0.05	0.10	0.20	0.30
0.05	-*- * *	7.9644	7.9422	7.8975	7.8075	7.7164
0.25	*	11.8988	11.8236	11.6717	11.3616	11.0427
0.50	*	14.1220	13.9947	13.7366	13.2051	12.6511
0.75	*	15.6014	15.4232	15.0758	14.3449	13.5744
1.00	*	16.7389	15.5233	16.0835	15.1654	14-1875

DESIGN TABLES FOR MODE(1,1) OF FREE PLATE OF ASPECT RATIO= 8.0

RYX	*		POISIONS RATIO			
	* * *	0.025	0.05	0.10	0.20	0.30
0.05	-*- *	7.9729	7.9506	7.9056	7.8156	7.724
0.25	*	11.9048	11.8295	11.6773	11.3665	11.047
0.50	*	14.1270	13.9996	13.7413	13.2093	12.654
0.7	*	15.6059	15.4326	15.0799	14.3485	13.577
1.0	*	16.7431	16.5274	16.0873	15.1685	14.190

DESIGN TABLES FOR MODE(1.1) OF FREE PLATE OF ASPECT RATIO= 9.0

*	RYX	*	PDISIONS RATIO					
* *		* *	0.025	0.05	0.10	0.20	0.30	
		*						
* *	0.05	*	7.9789	7.9566	7.9116	7.8212	7.7296	
<b>k</b>	0.25	*	11.9089	11-8335	11.6812	11.3704	11.0508	
k k	0.50	*	14.1305	14-0030	13.7445	13.2121	12.6572	
	0.75	*	15.6090	15-4356	15.0828	14.3509	13.5794	
۲ ۲	1.00	*	16.7460	16.5302	16.0899	15.1707	14.1918	

DESIGN TABLES FOR MODE(1,1) OF FREE PLATE OF ASPECT RATIO= 10.0

1	RYX	*		PDIS	PDISIONS RATIO		
		* * *	0.025	0.05	0.10	0.20	0.30
_	0.05	-*- * *	7.9833	7.9639	7.9160	7.8253	7.7336
	0.25	-	11.9119	11.3354	11.6840	11.3730	11.0532
	0.50	* *	14.1330	14.0055	13.7468	13.2142	12.6590
	0.75		15.6113	15.4378	15.0848	14.3527	13.5809
	1.00	. 1	16.7481	16.5322	16.0917	15.1723	14.1931

#### APPENDIX II

TABLE 6 VALUE OF  $\epsilon_{ extbf{r}}$ 

r	Clampe <b>d</b> -free	Free_free
1	1.8751041	Ο
2	4.6940911	0
3	7.8547574	4.7300408
4	10.9955407	7.8532046
5	14.1371684	10.9956078
6	$(2r - 1) \pi/2$	14.1371655
7	for r > 5	17.2787594
8		$(2r - 3) \pi/2$
		for $r > 7$

TABLE 7 INTEGRALS OF CHARACTERISTIC FUNCTIONS OF CLAMPED-FREE BEAM

Value of 
$$1 \int_{0}^{1} \frac{d \mathscr{D}_{r}}{dx} \frac{d \mathscr{D}_{s}}{dx} dx$$

		18 kg (18 18 18 18 18 18 18 18 18 18 18 18 18 1				
r	/s		2	3	4	5
	1	4.64778	-7.37987	3.94151	-6.59339	4.59198
	2		32.41735	-22.35243	13.58245	-22.83952
	3			77.29899	-35.64827	20.16205
	4				142.90185	-48.71964
	5	SYM	METRI	) A L		228.13325

Value of 
$$1 \int_{0}^{1} \phi_{r} \frac{d^{2} \phi_{s}}{dx^{2}} dx$$

r/s	1	2	3	4	5
1	0.85824	-11.74322	27.45315	-37.39025	51.95662
2	1.87385	-13.29425	-9.04222	30.40119	-33.70907
3	1.56451	3.22933	-45.90423	<b>-</b> 8.33537	36.38656
4	1.08737	5.54065	,4.25360	-98.91821	-7.82895
5	0.91404	3.71642	11.23264	4.73605	-171.58466

#### TABLE 8 INTEGRALS OF CHARACTERISTIC FUNCTIONS OF FREE-FREE BEAM

Values of 
$$1 \int_{0}^{1} \frac{d \mathscr{D}_{r}}{dx} \frac{d \mathscr{D}_{s}}{dx} dx$$

r/s	1	2	3	4	5
1	0	0	0	0	0
2	0	12.00000	0	13.85641	0
3	0	0	49.48082	0	35.37751
4	0	13.85641	0	1 <b>09.</b> 92459	0
5	0	0.00	35.37751	0	186.86671

Values of 
$$1 \int_{0}^{1} \phi_{\underline{x}} \frac{d^{2}\phi_{s}}{dx^{2}} dx$$

r/s	1	2	3	4	5
1	0	0.	18.58910	0	43.98096
2	0	0	0	40.59448	0
3	0	Ō	_12.30262	0	52.58440
4	0	O	0	-46.05012	0
5	O	0	1.80069	0	-98.90480